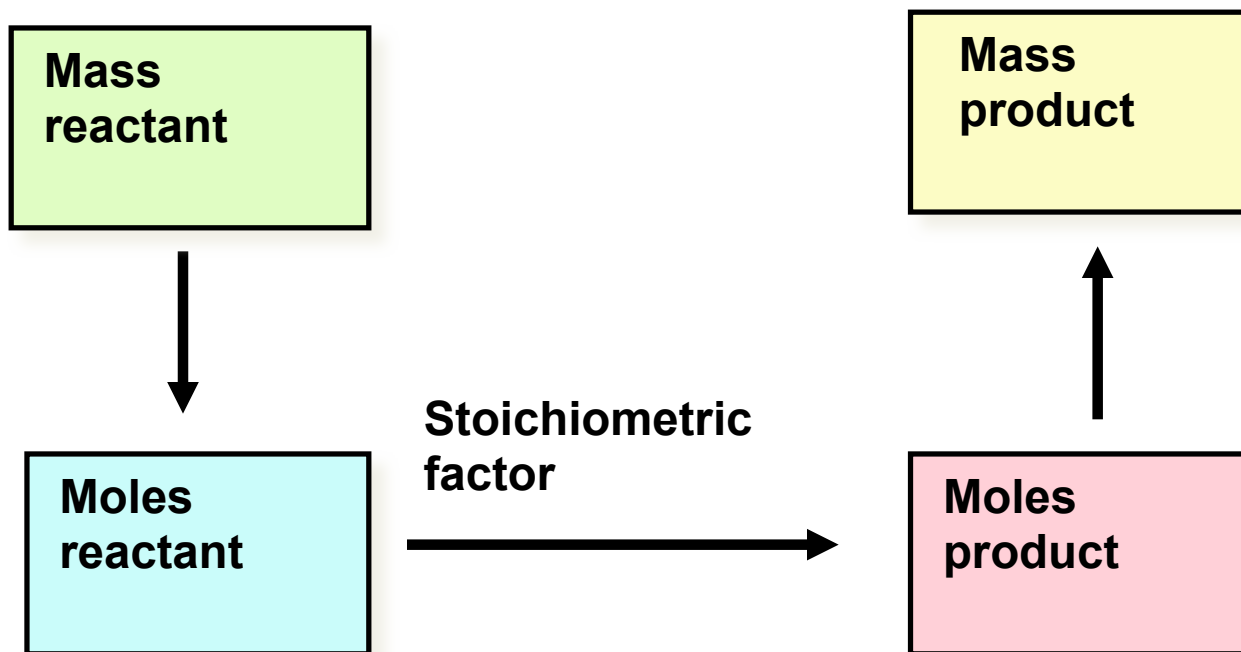


STOICHIOMETRY

– the study of the quantitative aspects of chemical

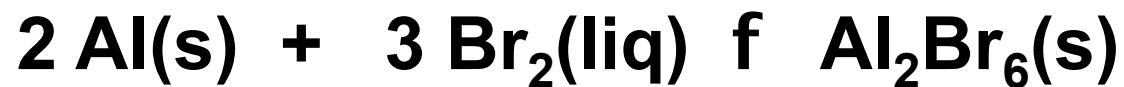
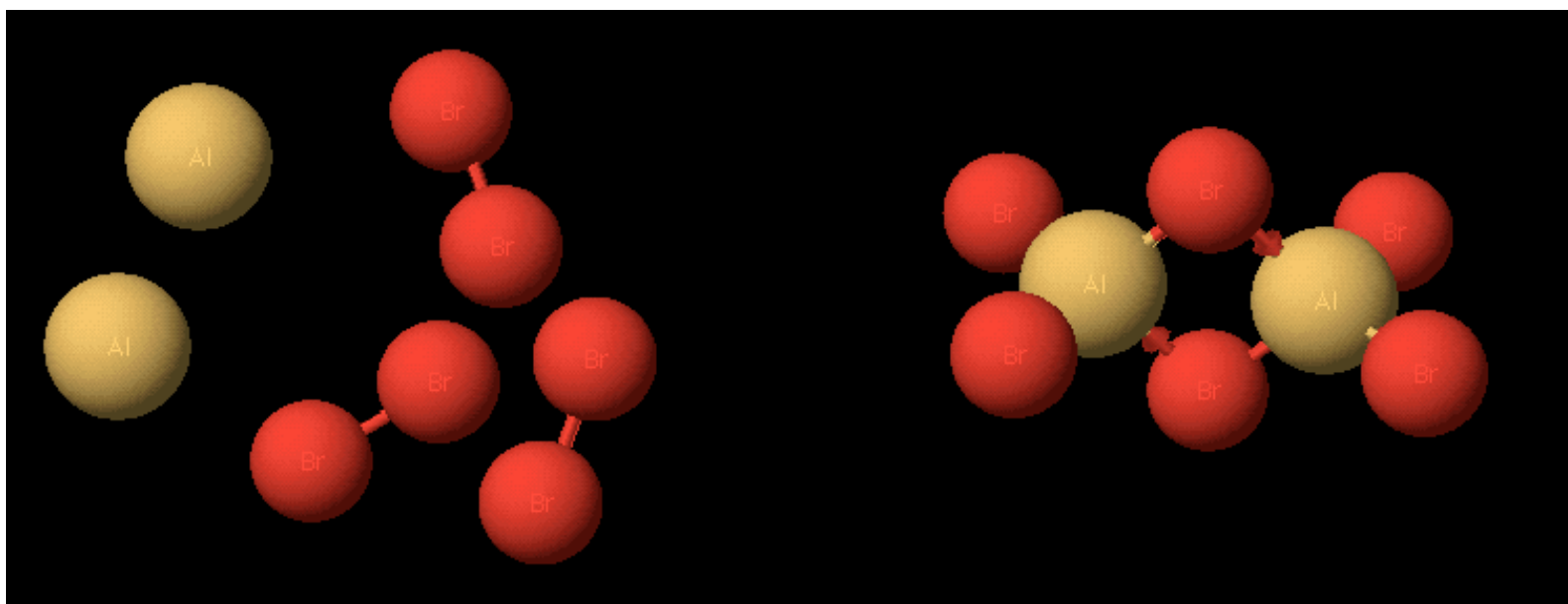


GENERAL PLAN FOR STOICHIOMETRY



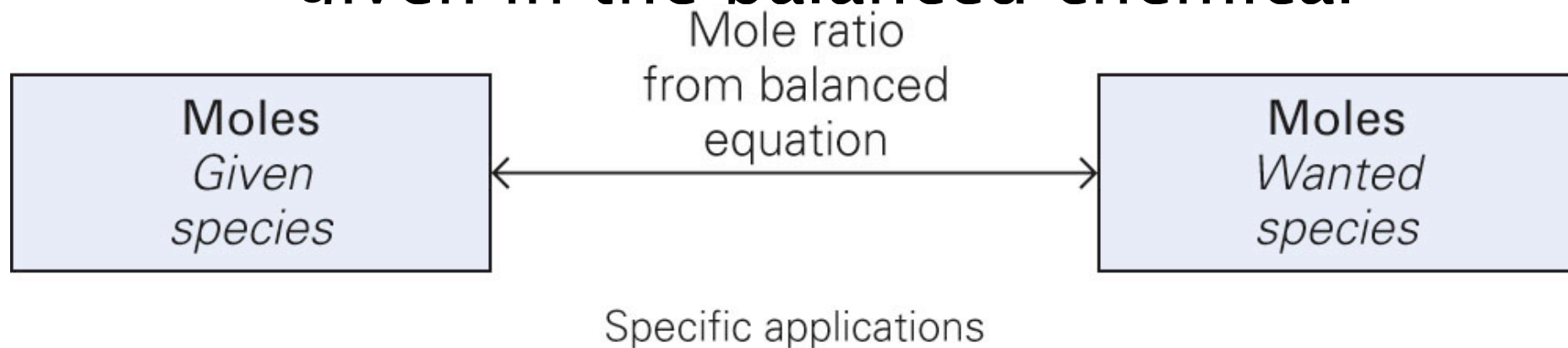
STOICHIOMETRY

It rests on the principle of the **conservation**



Conversion Factors from Eqns

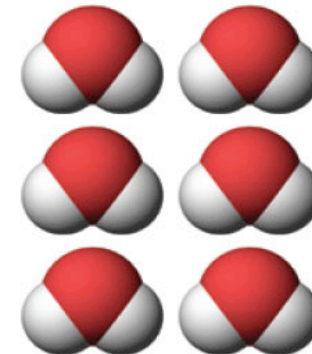
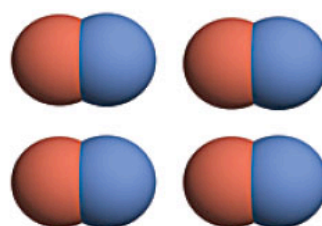
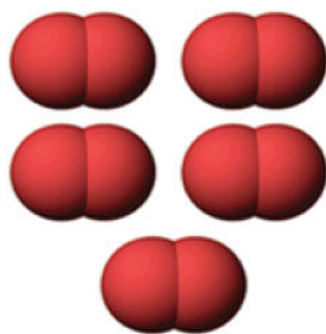
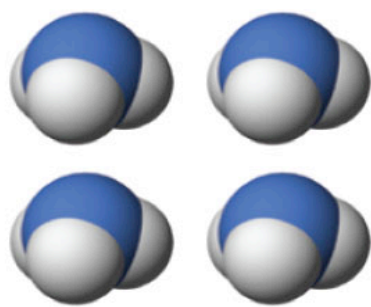
The mole ratio between two species, as given in the balanced chemical



Conversion Factors from Eqns

Example:

How many moles of oxygen are needed to completely react with 2.34 moles of ammonia in a reaction that yields nitrogen monoxide and water?



Conversion Factors from Eqns

How many moles of oxygen are needed to completely react with 2.34 moles of ammonia in a reaction that yields nitrogen monoxide and water?



$$\frac{5 \text{ mol O}_2}{4 \text{ mol NH}_3}$$

The P_{ER} relationship comes from the balanced equation:

Conversion Factors from Eqns

GIVEN: 2.34 mol NH₃, 4 NH₃ + 5 O₂ → 4 NO + 6 H₂O

WANTED: mol O₂ $\frac{5 \text{ mol O}_2}{4 \text{ mol NH}_3}$ →

PER:

$$\frac{5 \text{ mol O}_2}{4 \text{ mol NH}_3}$$

Mass–Mass Stoichiometry

Goal 2

Given a chemical equation, or a reaction for which the equation can be written, and the number of grams or moles of one species in the reaction, find the number of grams or moles of any other species.

Mass–Mass Stoichiometry

Stoichiometry

The quantitative relationships among substances involved in a chemical reaction.

Established by the balanced equation for the reaction.

A stoichiometry problem asks,
“How much or how many?”

Mass–Mass Stoichiometry

Prerequisite Skills for Stoichiometry

Write chemical formulas. Ch. 6

Calculate molar masses from chemical formulas. Sect. 7.4

Use molar masses to convert between moles and mass. Sect. 7.5

Write and balance chemical equations. Ch. 8

Use an equation to convert from moles

Mass–Mass Stoichiometry

How to Solve a Stoichiometry Problem: The Stoichiometry Path

Step 1: Change the mass of the given species to moles.

Step 2: Change the moles of the given species to the moles of the wanted species.

Step 3: Change the moles of the wanted species

Mass-Mass Stoichiometry

$$10.0 \text{ g } \cancel{\text{CH}_4} \times \frac{1 \text{ mol } \cancel{\text{CH}_4}}{16.04 \text{ g } \cancel{\text{CH}_4}} \times \frac{1 \text{ mol } \cancel{\text{CO}_2}}{1 \text{ mol } \cancel{\text{CH}_4}} \times \frac{44.01 \text{ g } \text{CO}_2}{\cancel{\text{mol CO}_2}} = 27.4 \text{ g}$$

CO₂

Percent Yield

Goal 3

Given two of the following, or information from which two of the following may be determined, calculate the third: theoretical yield, actual yield, percent yield.

Theoretical Yield = Maximum amount of product possible based on amount of reactant(s).

Actual Yield = How much product was actually obtained.

Percent Yield

The **actual yield** of a chemical reaction is usually less than the **theoretical yield** predicted by a stoichiometry calculation because:

- reactants may be impure
- the reaction may not go to completion
 - other reactions may occur

Actual yield is experimentally determined.

Percent Yield

Percent yield expresses the ratio of actual yield to theoretical yield:

$$\% \text{ yield} = \frac{\text{actual yield}}{\text{theoretical yield}} \times 100$$

Percent Yield

Example:

Determine the percent yield if 6.97 grams of ammonia is produced from the reaction of 6.22 grams of nitrogen with excess hydrogen.

Solution:

Notice that two quantities are given in the problem statement.

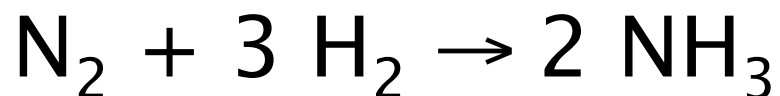
6.97 g NH_3 is the actual yield

6.22 g N_2 is the amount of reactant. This can be used to

Percent Yield

GIVEN: 6.22 g N₂
(theo)

WANTED: g NH₃



P_{ER}: $\xrightarrow{28.02 \text{ g N}_2 / \text{mol N}_2}$ $\xrightarrow{2 \text{ mol NH}_3 / 1 \text{ mol}}$
N₂
PATH: g N₂ $\xrightarrow{\hspace{10em}}$ mol N₂

Percent Yield

$$6.22 \text{ g N}_2 \times \frac{1 \text{ mol N}_2}{28.02 \text{ g N}_2} \times \frac{2 \text{ mol NH}_3}{1 \text{ mol N}_2} \times \frac{17.03 \text{ g NH}_3}{1 \text{ mol NH}_3} = 7.56 \text{ g NH}_3$$

(theo)

$$\begin{aligned} \% \text{ yield} &= \frac{\text{actual yield}}{\text{theoretical yield}} \times 100 \\ &= \frac{6.97 \text{ g NH}_3 \text{ (act)}}{7.56 \text{ g NH}_3 \text{ (theo)}} \times 100 = \end{aligned}$$

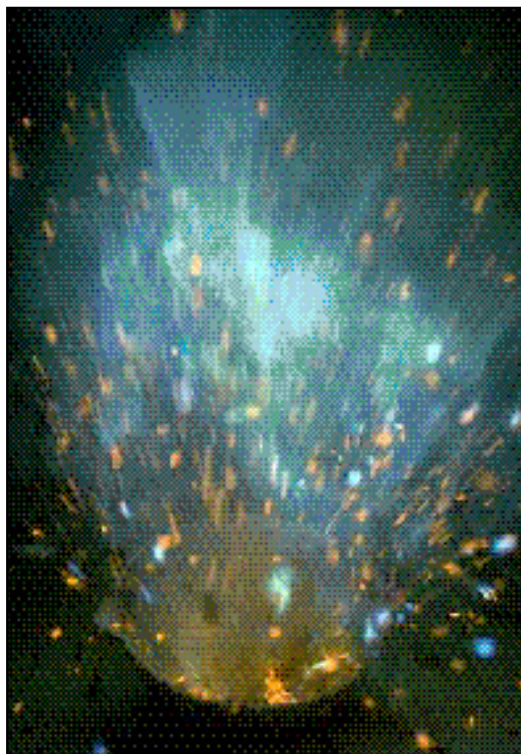
Percent Yield

Once a percent yield has been determined for a reaction, it can be used in stoichiometry calculations.

For example, the 92.2% yield from the prior example means:

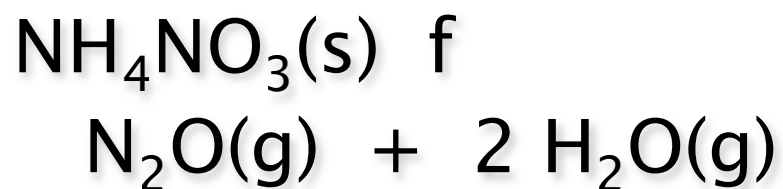
$$\frac{100 \text{ g (theo)}}{92.2 \text{ g (act)}}$$

PROBLEM: If 454 g of NH_4NO_3 decomposes, how much N_2O and H_2O are formed? What is the theoretical yield of products?



STEP 1

Write the balanced
chemical equation

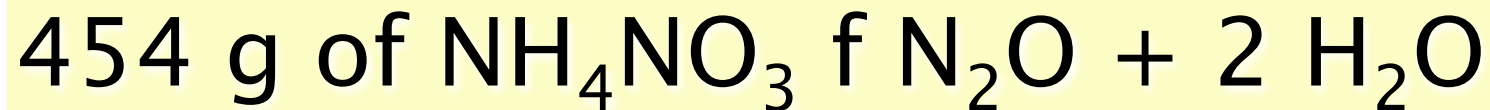


454 g of NH_4NO_3 f $\text{N}_2\text{O} + 2 \text{H}_2\text{O}$

STEP 2 Convert mass of reactant
(454 g) to amount (mol)

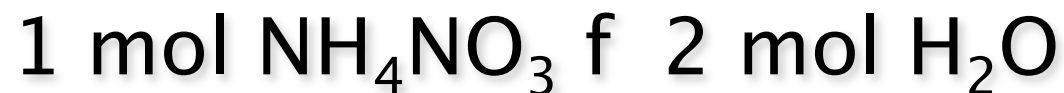
$$454 \text{ g} \left(\frac{1 \text{ mol}}{80.04 \text{ g}} \right) = 5.67 \text{ mol } \text{NH}_4\text{NO}_3$$

STEP 3 Convert amount of reactant
(5.67 mol) to amount (mol) of
product.



STEP 3 Convert moles reactant f
moles product

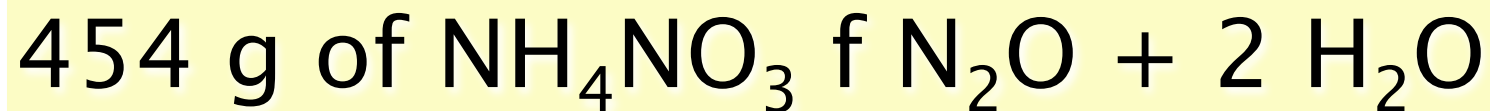
Relate moles NH_4NO_3 to moles
product expected.



Express this relation as the

STOICHIOMETRIC FACTOR

$$\frac{2 \text{ mol } \text{H}_2\text{O} \text{ produced}}{1 \text{ mol } \text{NH}_4\text{NO}_3 \text{ used}}$$



STEP 3 Convert moles reactant (5.67 mol) to amount (mol) of product

$$5.67 \text{ mol } \text{NH}_4\text{NO}_3 \left(\frac{2 \text{ mol } \text{H}_2\text{O} \text{ produced}}{1 \text{ mol } \text{NH}_4\text{NO}_3 \text{ used}} \right) \\ = 11.3 \text{ mol } \text{H}_2\text{O} \text{ produced}$$

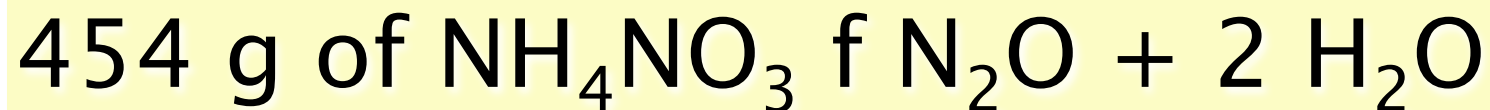
454 g of NH_4NO_3 f $\text{N}_2\text{O} + 2 \text{H}_2\text{O}$

STEP 4 Convert amount of product
(11.3 mol) to mass of product

Called the **THEORETICAL YIELD**

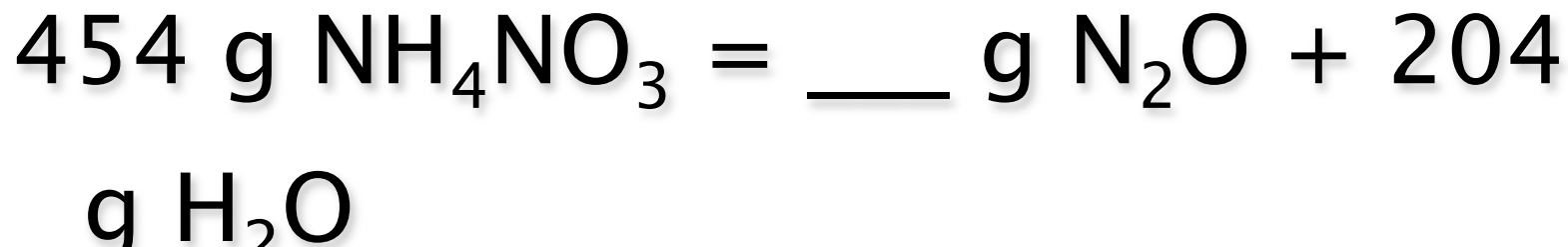
$$11.3 \text{ mol H}_2\text{O} \left(\frac{18.02 \text{ g}}{1 \text{ mol}} \right) = 204 \text{ g H}_2\text{O}$$

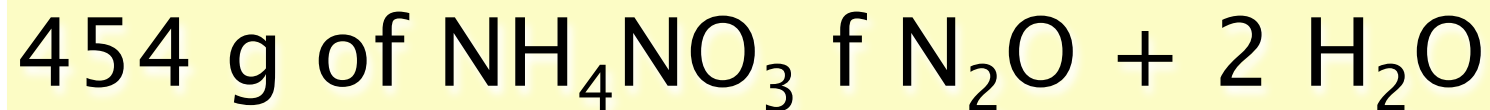
**ALWAYS FOLLOW THESE STEPS IN
SOLVING STOICHIOMETRY PROBLEMS!**



STEP 5 What mass of N_2O is formed?

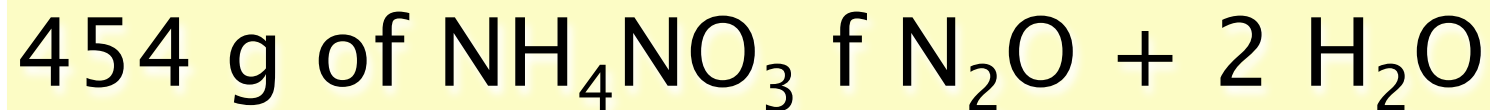
Total mass of reactants =
total mass of products





Amounts Table (from page 159)

1. Compound	NH_4NO_3	N_2O	H_2O
2. Initial (g)			
3. Initial (mol)			
4. Change (mol)			
5. Final (mol)			
6. Final (g)			



Amounts Table

1.Compound	NH_4NO_3	N_2O	H_2O
2.Initial (g)	454 g	0	0
3.Initial (mol)	5.67 mol	0	0
4.Change (mol)	-5.67	+5.67	+2(5.67)
5.Final (mol)	0	5.67	11.3
6.Final (g)	0	250	204

Note that matter is conserved!

454 g of NH_4NO_3 f N_2O + 2 H_2O

STEP 6 Calculate the **percent yield**

If you isolated only 131 g of N_2O ,
what is the percent yield?

This compares the **theoretical** (250.

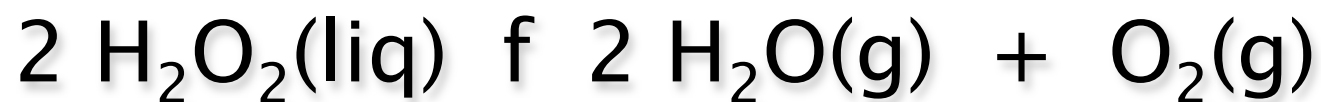
454 g of NH_4NO_3 f $\text{N}_2\text{O} + 2 \text{H}_2\text{O}$

STEP 6 Calculate the percent yield

$$\% \text{ yield} = \frac{\text{actual yield}}{\text{theoretical yield}} \times 100\%$$

$$\% \text{ yield} = \left(\frac{131 \text{ g}}{250. \text{ g}} \right) \times 100\% = 52.4\%$$

PROBLEM: Using 5.00 g of H_2O_2 , what mass of O_2 and of H_2O can be obtained?



Reaction is catalyzed by MnO_2

Step 1: amount (mol) of H_2O_2

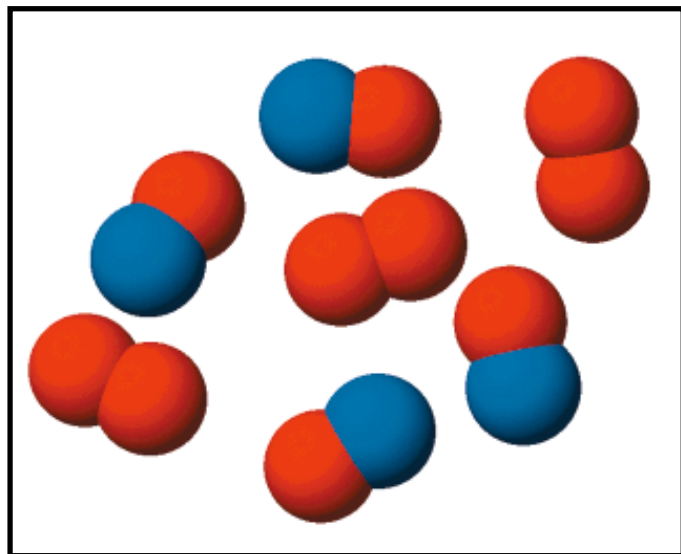
Step 2: use **STOICHIOMETRIC FACTOR** to calculate amount (mol) of O_2

Reactions Involving a **LIMITING REACTANT**

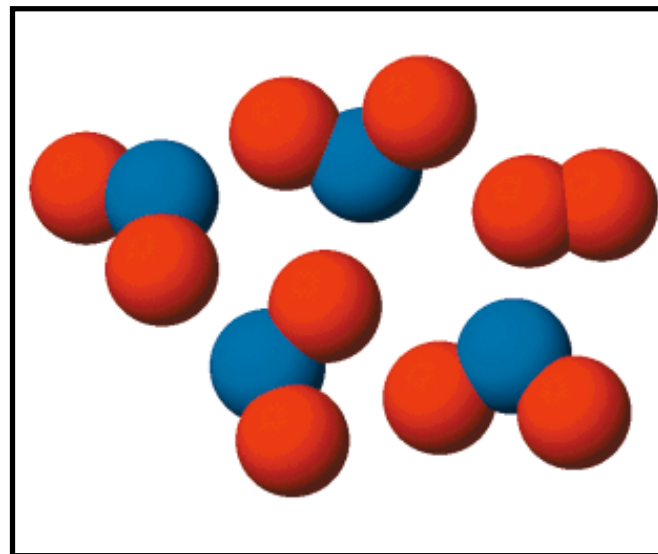
1. In a given reaction, there is not enough of one reagent to use up the other reagent completely.
2. The reagent in short supply **LIMITS** the quantity of product that can be formed.



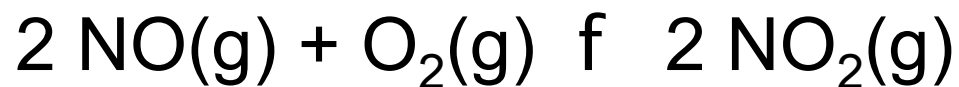
LIMITING REACTANTS



Reactants



Products



Limiting reactant = _____

Excess reactant = _____

LIMITING REACTANTS



React solid Zn with 0.100 mol HCl (aq)



1 **2** **3**

Rxn 1: Balloon inflates fully, some Zn left

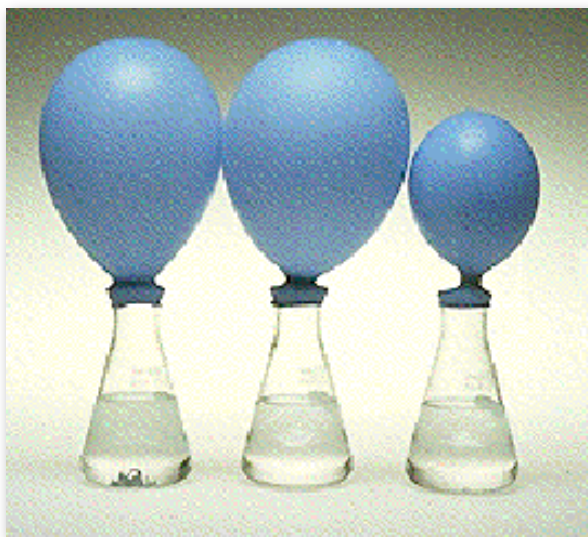
* More than enough Zn to use up the 0.100 mol HCl

Rxn 2: Balloon inflates fully, no Zn left

* Right amount of each (HCl and Zn)

Rxn 3: Balloon does not inflate fully, no Zn left.

LIMITING REACTANTS



React solid Zn with 0.100 mol
HCl (aq)



0.10 mol HCl [1 mol Zn/2 mol HCl]
= 0.050 mol Zn

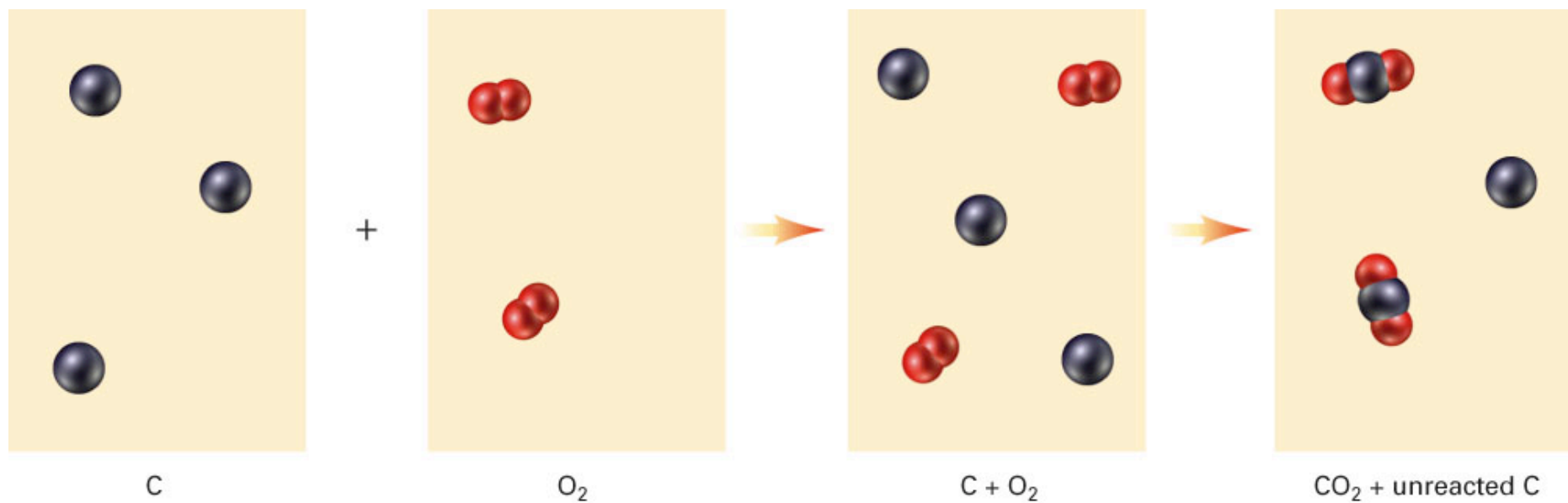
	Rxn 3	Rxn 1	Rxn
2			
mass Zn (g)		7.00	3.27
1.31			
mol Zn		0.107	
0.050		0.020	

Limiting Reactants

Goal 4

Identify and describe or explain limiting reactants and excess reactants.

Limiting Reactants

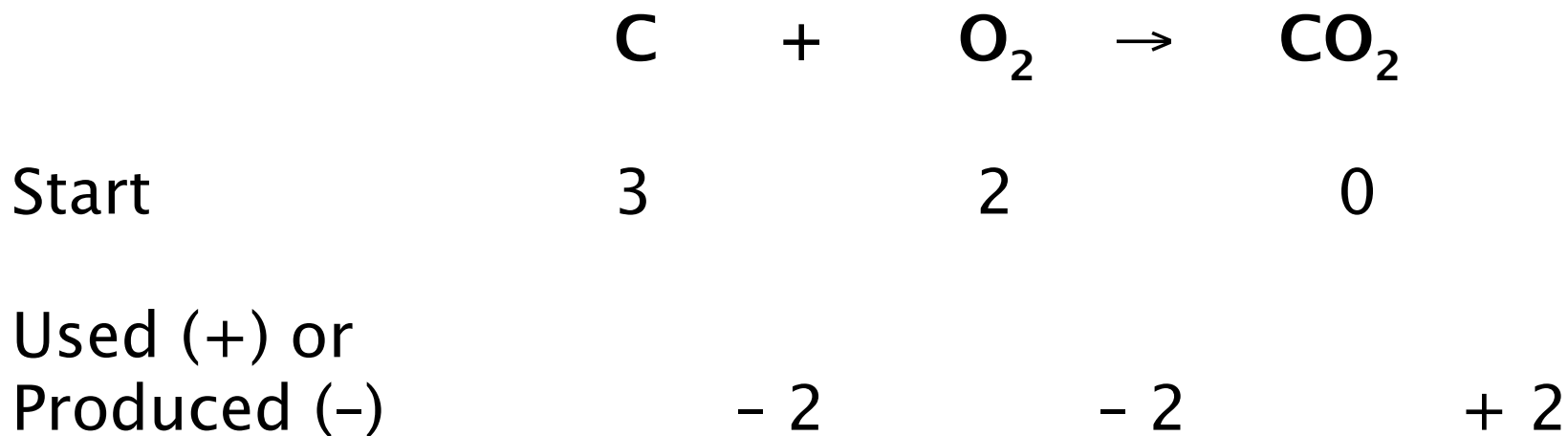


Three atoms of carbon react with two molecules of oxygen:

Limiting Reactants

The reaction will stop when two molecules of oxygen are used up.

Two carbon dioxide molecules will form;
One carbon atom will remain unreacted:



Limiting Reactants

Limiting Reactant

The reactant that is completely used up.
(Oxygen)

Excess Reactant

The reactant initially present in excess.
(some will remain unreacted)
(Carbon)

Limiting Reactants

Goal 5

Given a chemical equation, or information from which it may be determined, and initial quantities of two or more reactants, (a) identify the limiting reactant, (b) calculate the theoretical yield of a specified product, assuming complete use of the limiting reactant, and (c) calculate the quantity of reactant initially in excess that remains unreacted.

Limiting Reactants

Comparison-of-Moles Method

How to Solve a Limiting Reactant Problem:

1. Convert the number of grams of each reactant to moles.
2. Identify the limiting reactant.
3. Calculate the number of moles of each species that reacts or is produced.
4. Calculate the number of moles of each species that remains after the reaction.
5. Change the number of moles of each species to grams.

Limiting Reactants

Example:

A 24.0-g piece of solid sodium is added to 24.0 g of liquid water. How many grams of hydrogen will be produced? How many grams of which reactant will be left over?

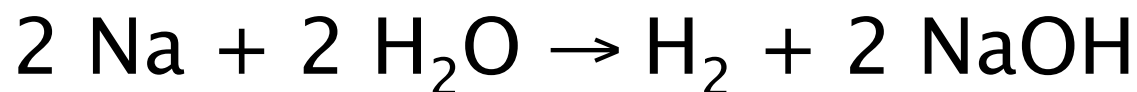
Solution:

Step 1 is to convert the number of grams of each reactant to moles.

$$24.0 \text{ g Na} \times \frac{1 \text{ mol Na}}{22.99 \text{ g Na}} = 1.04 \text{ mol Na}$$
$$\frac{1 \text{ mol H}_2\text{O}}{18.02 \text{ g H}_2\text{O}}$$

Limiting Reactants

Step 2 is to identify the limiting reactant. This requires a balanced chemical equation so that the mole ratio of the reacting substances can be identified.



For every 2 mol of Na that react, 2 mol of H₂O react, a 2:2 or 1:1 ratio. Thus, the 1.04 mol Na will be the limiting reactant.

Limiting Reactants

Step 3 is to calculate the number of moles of each species that reacts or is produced. This can be done by assembling the data into a table.

	2 Na +	2 H ₂ O	→ H ₂	+ 2
NaOH				
Grams at start	24.0	24.0	0	0
Molar mass, g/mol		22.99	18.02	
	2.016	40.00		
Moles at start		1.04	1.33	
	0	0		
Moles used	(-) $\frac{1 \text{ mol H}_2}{2 \text{ mol Na}}$			

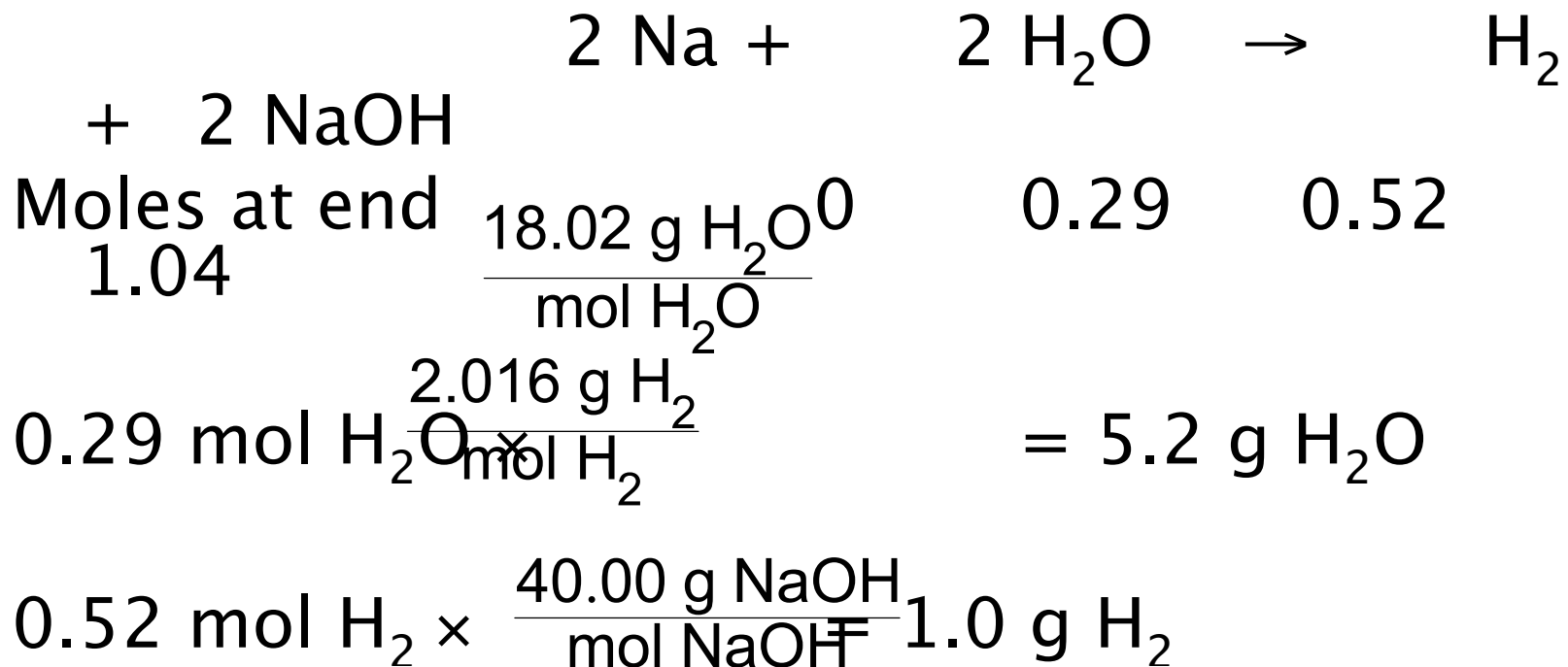
Limiting Reactants

Step 4 is to calculate the number of moles of each species that remains after the reaction.

	2 Na +	2 H ₂ O	→	H ₂
+ 2 NaOH				
Grams at start	24.0	24.0		0
0				
Molar mass, g/mol	22.99		18.02	
2.016	40.00			
Moles at start	1.04	1.33		0

Limiting Reactants

Step 5 is to change the number of moles of each species to grams.



Limiting Reactants

Returning to the original problem statement:

A 24.0-g piece of solid sodium is added to 24.0 g of liquid water. How many grams of hydrogen will be produced? How many grams of which reactant will be left over?

The questions can now be answered:

1.0 g H₂ is produced

Limiting Reactants

Goal 5

Given a chemical equation, or information from which it may be determined, and initial quantities of two or more reactants, (a) identify the limiting reactant, (b) calculate the theoretical yield of a specified product, assuming complete use of the limiting reactant, and (c) calculate the quantity of reactant initially in excess that remains unreacted.

Limiting Reactants

Smaller-Amount Method

How to Solve a Limiting Reactant Problem:

1. Calculate the amount of product that can be formed by the initial amount of each reactant.
 - a) The reactant that yields the smaller amount of product is the limiting reactant.
 - b) The smaller amount of product is the amount that will be formed when all of the limiting reactant is used up.
2. Calculate the amount of excess reactant that is used by the total amount of limiting reactant.
3. Subtract from the amount of excess reactant present initially the amount that is used by all of

Limiting Reactants

Example:

A 24.0-g piece of solid sodium is added to 24.0 g of liquid water. How many grams of hydrogen will be produced? How many grams of which reactant will be left over?

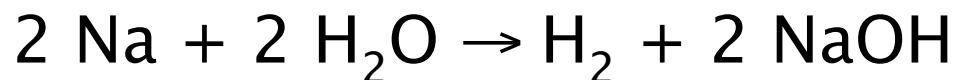
Solution:

Step 1 is to calculate the amount of product that can be formed by the initial amount of each reactant.

Limiting Reactants

GIVEN: 24.0 g Na

WANTED: g H₂



$$24.0 \text{ g Na} \times \frac{1 \text{ mol Na}}{22.99 \text{ g Na}} \times \frac{1 \text{ mol H}_2}{2 \text{ mol Na}} \times \frac{2.016 \text{ g H}_2}{1 \text{ mol H}_2} = 1.05 \text{ g H}_2$$

$$\text{GIVEN: } 24.0 \text{ g H}_2\text{O} \times \frac{1 \text{ mol H}_2\text{O}}{18.02 \text{ g H}_2\text{O}} \times \frac{1 \text{ mol H}_2}{2 \text{ mol H}_2\text{O}} \times \frac{2.016 \text{ g H}_2}{1 \text{ mol H}_2}$$

$$24.0 \text{ g H}_2\text{O} \times \quad \times \quad \times$$

Limiting Reactants

24.0 g Na and excess H₂O
produces 1.05 g H₂

24.0 g H₂O and excess Na
produces 1.34 g H₂

Step 1a: The reactant that yields the smallest amount of product is the limiting reactant, so Na is the limiting reactant.

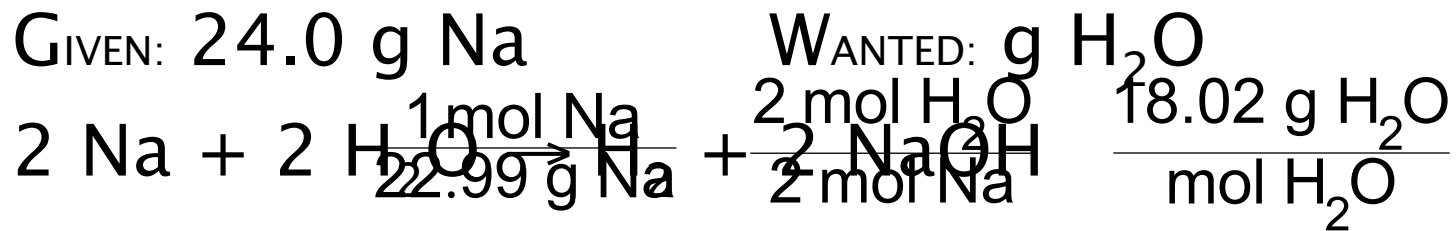
Step 1b: The smaller amount of product is the amount that will be formed when all of the limiting reactant is

Limiting Reactants

Step 2 is to calculate the amount of excess reactant that is used by the total amount of limiting reactant.

The total amount of limiting reactant is 24.0 g Na.

The excess reactant is H₂O.

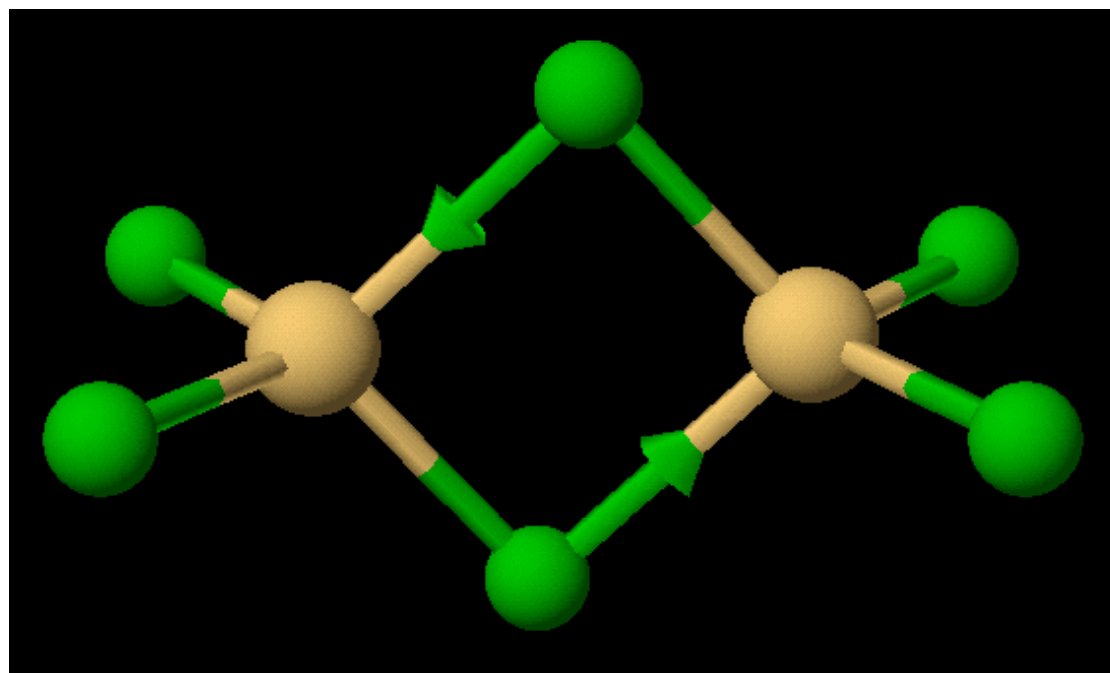
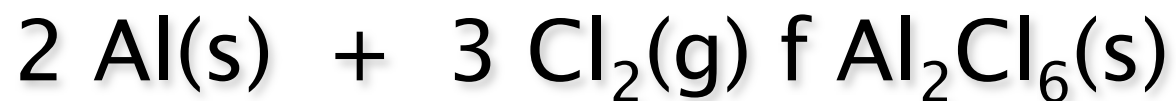


Limiting Reactants

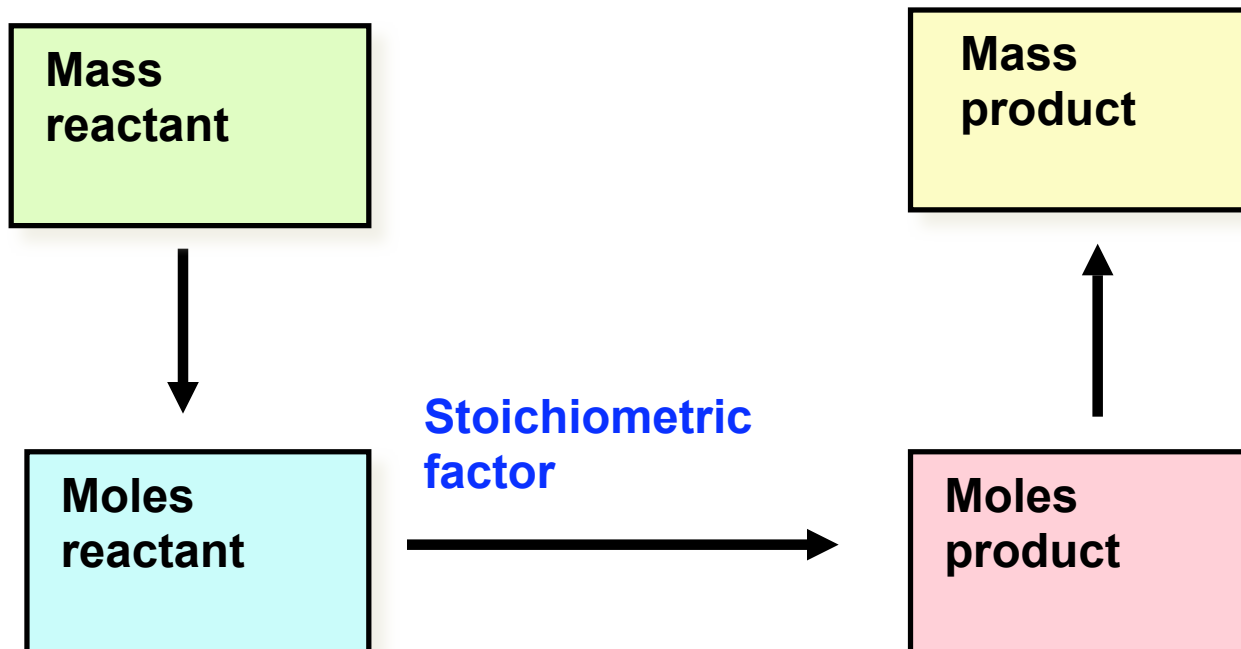
Step 3 is to subtract from the amount of excess reactant present initially the amount that is used by all of the limiting reactant. The difference is the amount of excess reactant left.

$$\begin{array}{r} 24.0 \text{ g H}_2\text{O initially} \\ - \overline{18.8 \text{ g H}_2\text{O reacted}} \end{array}$$

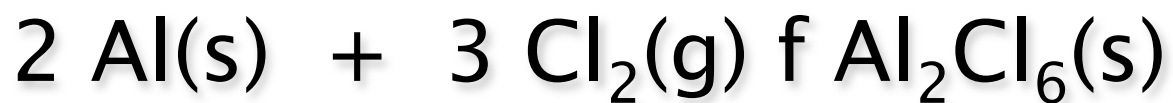
Reaction to be Studied



PROBLEM: Mix 5.40 g of Al with 8.10 g of Cl_2 . What mass of Al_2Cl_6 can form?



**Step 1 of LR problem:
compare actual mole ratio of
reactants to theoretical mole
ratio.**



Reactants must be in the mole

$$\frac{\text{mol Cl}_2}{\text{mol Al}} = \frac{3}{2}$$

Step 2 of LR problem: Calculate moles of each reactant

We have 5.40 g of Al and 8.10 g of Cl₂

$$5.40 \text{ g Al} \left(\frac{1 \text{ mol}}{27.0 \text{ g}} \right) = 0.200 \text{ mol Al}$$

$$8.10 \text{ g Cl}_2 \left(\frac{1 \text{ mol}}{70.9 \text{ g}} \right) = 0.114 \text{ mol Cl}_2$$

Find mole ratio of reactants



$$1. \frac{0.200 \text{ mol Al} \times \frac{3 \text{ mol Cl}_2}{2 \text{ mol Al}}}{\text{mol Cl}_2} = 0.300$$

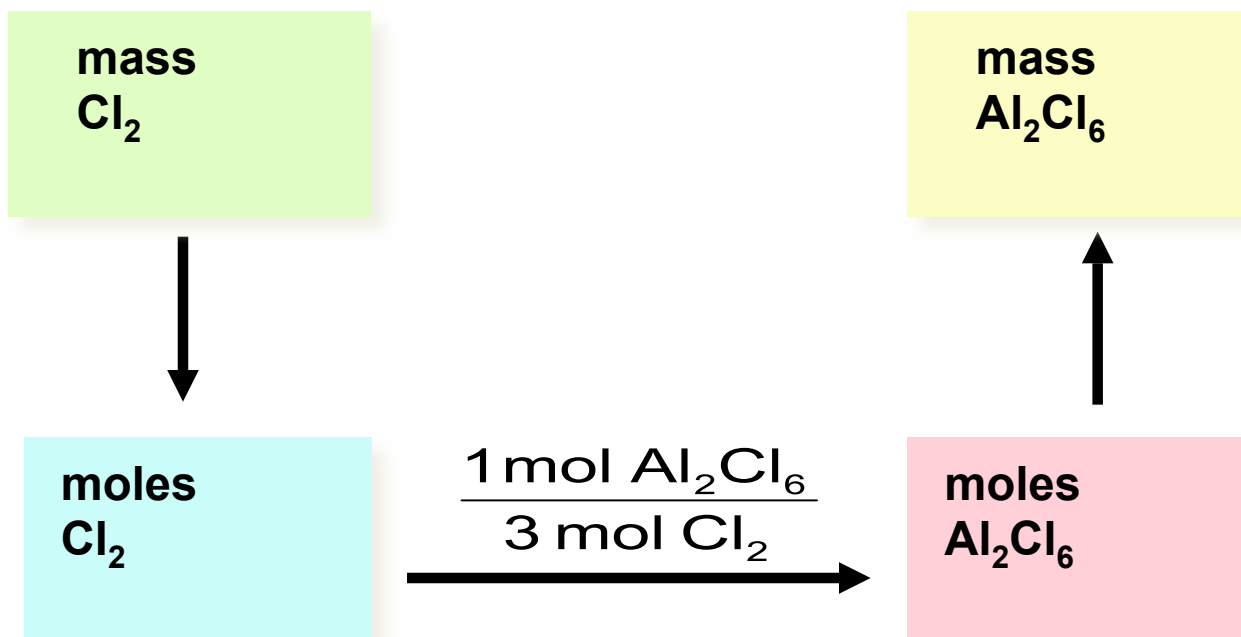
2. needed to react with 0.200 mol Al, but we only have 0.114 mole of Cl_2 , so

Limiting reactant is Cl_2

Mix 5.40 g of Al with 8.10 g of Cl₂. What mass of Al₂Cl₆ can form?



Limiting reactant = Cl₂
Base all calcs. on Cl₂



CALCULATIONS: calculate mass of Al_2Cl_6 expected.

Step 1: Calculate moles of Al_2Cl_6 expected based on LR.

$$0.114 \text{ mol Cl}_2 \left(\frac{1 \text{ mol Al}_2\text{Cl}_6}{3 \text{ mol Cl}_2} \right) = 0.0380 \text{ mol Al}_2\text{Cl}_6$$

Step 2: Calculate mass of Al_2Cl_6 expected based on LR.

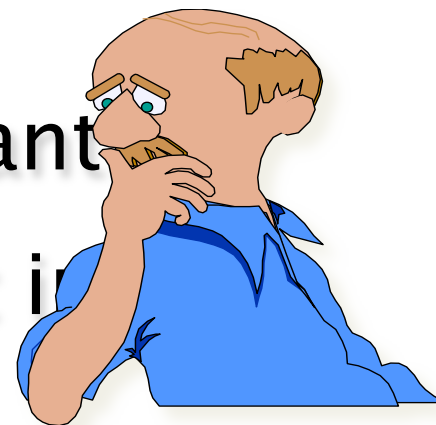
$$0.0380 \text{ mol Al}_2\text{Cl}_6 \left(\frac{266.4 \text{ g Al}_2\text{Cl}_6}{\text{mol}} \right) = 10.1 \text{ g Al}_2\text{Cl}_6$$

How much of which reactant will remain when reaction is complete?

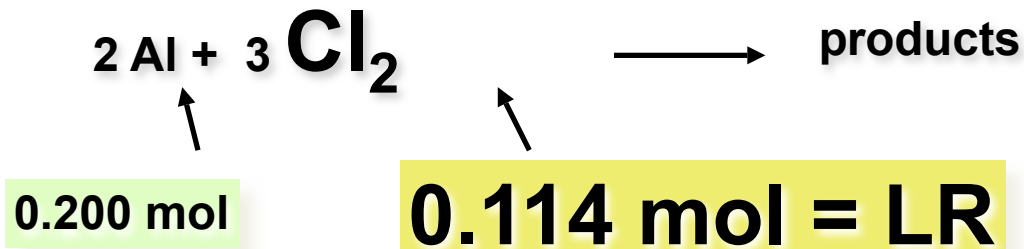
1. Cl_2 was the limiting reactant

Therefore, Al was present in excess. But how much?

2. First find how much Al was required.



Calculating Excess Al



$$0.114 \text{ mol Cl}_2 \left(\frac{2 \text{ mol Al}}{3 \text{ mol Cl}_2} \right) = 0.0760 \text{ mol Al req'd}$$

$$\text{Excess Al} = \text{Al available} - \text{Al required}$$

$$= 0.200 \text{ mol} - 0.0760 \text{ mol}$$

$$= 0.124 \text{ mol Al in excess}$$

Energy

Goal 6

Given energy in one of the following units, calculate the other three: joules, kilojoules, calories, and kilocalories.

Energy

Energy

The ability to do work or transfer heat.

Energy Unit: Joule

Joule (J)

The amount of energy exerted when a force of one newton (force required to cause a mass of 1 kg to accelerate at a rate of 1 m/s²) is applied over a displacement of one meter:

$$1 \text{ joule} = 1 \text{ newton} \times 1 \text{ meter}$$

$$1 \text{ J} = 1 \text{ kg} \cdot \text{m}^2/\text{sec}^2$$

Energy

Energy Unit: Calorie

calorie (historical definition):
Amount of energy required to raise the
temperature of 1 g of water by 1°C.

calorie (modern definition)
1 cal \equiv 4.184 J

A food Calorie (Cal) is a thermochemical kilocalorie.
In scientific writing it is capitalized;
in everyday writing, interpret the context.

1 kcal = 4.184 kJ

Energy

Example:

How many joules are equivalent to 2.4×10^2 food Calories?

Solution:

A food Calorie is a thermochemical kilocalorie.

$$\begin{array}{l} \text{GIVEN: } 2.4 \times 10^2 \text{ kcal} \qquad \qquad \qquad \text{WANTED: J} \\ \text{PER: } \qquad \qquad \frac{1000 \text{ cal}}{\text{kcal}} \qquad \qquad \qquad \frac{4.184 \text{ J}}{\text{cal}} \\ \text{PATH: kcal} \qquad \qquad \frac{1000 \text{ cal}}{\text{kcal}} \qquad \frac{4.184 \text{ J}}{\text{cal}} \qquad \qquad \qquad \text{J} \end{array}$$

Thermochemical Equations

Goal 7

Given a chemical equation, or information from which it may be written, and the heat (enthalpy) of reaction, write the thermochemical equation either (a) with ΔH to the right of the conventional equation or (b) as a reactant or product.

Thermochemical Equations

Enthalpy

Heat content of a system.

Symbol: H

ΔH is the enthalpy of reaction, or, as chemists commonly call it, the heat of reaction.

Δ means “change in”:

It is determined by subtracting the initial quantity from the final quantity:
 $\Delta A = \text{final value of } A - \text{initial value of } A$

Thermochemical Equations

Enthalpy of Reaction, ΔH

If the final heat content of a system is less than its initial heat content, ΔH is negative, and the change is exothermic.

If the final heat content of a system is greater than its initial heat content, ΔH is positive, and the change is endothermic.

Thermochemical Equations

Thermochemical Equation

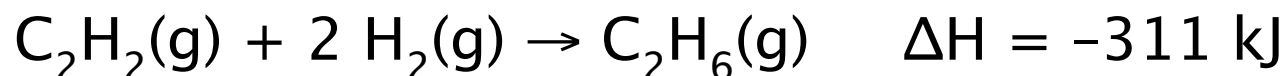
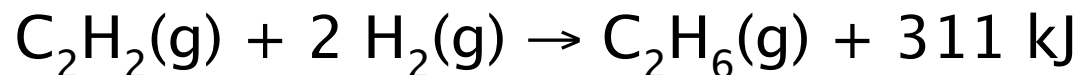
A conventional equation plus its associated ΔH term.

Thermochemical equations are typically written in one of two different ways, depending on the context for which it is needed.

Example:

When one mole of acetylene gas reacts with two moles of hydrogen gas, one mole of ethane gas is formed and 311 kJ of energy is released. Write the thermochemical equation in two forms.

Solution:



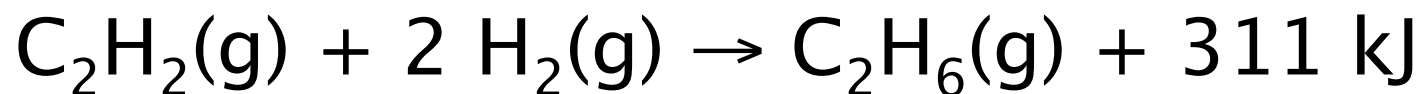
Thermochem Stoichiometry

Goal 8

Given a thermochemical equation, or information from which it may be written, calculate the amount of energy released or added for a given amount of reactant or product; alternately, calculate the mass of reactant required to produce a given amount of energy.

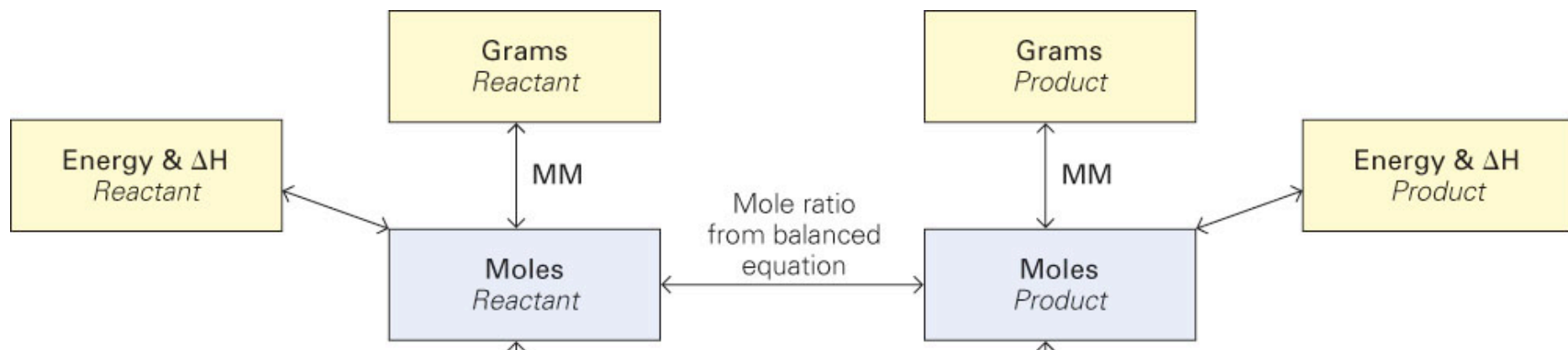
Thermochem Stoichiometry

The energy term in a thermochemical equation is directly proportional to the number of moles of all species in the reaction.



$$311 \text{ kJ} \propto 1 \text{ mol C}_2\text{H}_2$$

Thermochem Stoichiometry



Thermochem Stoichiometry

Example:

When propane, $\text{C}_3\text{H}_8(\text{g})$, is burned to form gaseous carbon dioxide and liquid water, 2.22×10^3 kJ of heat is released for every mole of propane burned. What quantity of heat is released when 1.00×10^2 g of propane is burned?

Solution:

First, write and balance the thermochemical equation to determine the stoichiometric relationships.

Thermochem Stoichiometry

GIVEN: 1.00×10^2 g C_3H_8
of heat

WANTED: quantity

(assume kJ)

PER: $\frac{1 \text{ mol } C_3H_8}{44.09 \text{ g } C_3H_8}$

PATH: $\frac{\text{g } C_3H_8}{C_3H_8} \rightarrow \text{mol}$

$$\frac{2.22 \times 10^2 \text{ g } C_3H_8}{44.09 \text{ g } C_3H_8} \times \frac{1 \text{ mol } C_3H_8}{1 \text{ mol } C_3H_8} = 5.04 \text{ mol } C_3H_8$$