# On semantics of STRIPS By Vladimir Lifschitz

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#### Outline

Introduction to STRIPS

Semantics of STRIPS

#### The STRIPS

- STRIPS: n. 1) An automated planner by Fikes and Nilsson in 1971 2) The input language of the planner.
- It operates on world models, represented by sets of formulas of first-order logic.
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# Building blocks of STRIPS

- Start with an arbitrary first-order language L.
- A world model is any set of sentences of L.
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### An example

modified from original STRIPS paper

### operator pushto(X, Y): robot pushes object X next to Y

- Precondition:  $pushable(X) \land next to(robot, X)$
- Delete list: atrobot(\$), nextto(robot,\$), nextto(\$, X), at(X,\$), nextto(X,\$)
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- A plan defines a sequence of world models  $M_0, M_1, \ldots, M_N$ , where  $M_0$  is the initial world model and  $M_i = (M_{i-1} \setminus D_{\alpha_i}) \cup A_{\alpha_i}$ ,  $\forall i \in 1..N$ .
- $\bar{\alpha}$  is accepted by the system if  $M_{i-1} \vdash P_{\alpha_i}$ ,  $\forall i \in 1..N$ .
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- The world described by language L at any instant is in a *state*.
- An action is a partial function from from states to states.
- If f(s) is defined, we say that f is applicable in state s and f(s) is the result of action f.
- We assume that each operator  $\alpha$  in STRIPS is associated with an action  $f_{\alpha}$ .
- A STRIPS system along with the information above is called an interpreted STRIPS system.
- For each plan  $\bar{\alpha}=(\alpha_1,\ldots,\alpha_N)$  of an interpreted STRIPS system, we define  $f_{\bar{\alpha}}$  to be the composite action  $f_{\alpha_N}\ldots f_{\alpha_1}$ .

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#### How sound is STRIPS in describing a world?

#### Definition A

An operator description (P, D, A) is sound relative to an action f if for every state s such that P is satisfied in s,

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#### Soundness cond.

Is this semantics good?

#### **Problems**

- Atoms in the delete list of pushto(X, Y) are obviously not the only sentences that may become false after action execution.
- Their conjunction or disjunction, e.g, atrobot(\$) ∧ nextto(X,\$), or any sentence of the form A ∧ F (A is an atom in delete list and F is any sentence in L) is also a such sentence. By definition A, the delete list will be infinite.
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- Thus, they have to be satisfied in all states.

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# Second try on semantics

#### Definition B

An operator description (P, D, A) is sound relative to an action f if, for every state s such that P is satisfied in s,

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- every atomic sentence that is satisfied in s and does not belong to D is satisfied in f(s),
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 $\Sigma$  is sound if  $M_0$  is satisfied in the initial state  $s_0$ , each operator description  $(P_{\alpha}, D_{\alpha}, A_{\alpha})$  is sound relative to  $f_{\alpha}$ , and every non-atomic sentence in  $M_0$  is satisfied in all states of the world.

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Suppose we have a special set E of ground atoms. Formulas from E is called *essential*.

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