TEXAS TECH UNIVERSITY TTU K-12

Mathematics, Grade 7, Second Semester<br>CBE Review

Online \#3716, 3717; Print \#10130, 10297 (v.3.0)

## To the Student:

After your registration is complete, you may take the Credit by Examination for MATH 7B. (If you are taking the print exam, your proctor must be approved.)

## WHAT TO BRING

- several sharpened No. 2 pencils
- lined notebook paper


## ABOUT THE EXAM

The examination for the second semester of Mathematics, Grade 7, consists of 45 multiple choice and problem-solving questions. The exam is based on the Texas Essential Knowledge and Skills (TEKS) for this subject. The full list of TEKS is included in this document (it is also available online at the Texas Education Agency website). The TEKS outline specific topics covered in the exam, as well as more general areas of knowledge and levels of critical thinking. Use the TEKS to focus your study in preparation for the exam. TEKS covered in this semester are indicated by a checkmark; the exam will focus on the checkmarked TEKS, but may touch on any of the full list.

The examination will take place under supervision, and the recommended time limit is three hours. A 7th grade mathematics chart is included in the exam for your reference. You may not use any other notes or books. A percentage score from the examination will be reported to the official at your school.

A list of key concepts is included in this document to focus your studies. It is important to prepare adequately. Since questions are not taken from any one source, you can prepare by reviewing any of the state-adopted textbooks that are used at your school. The digital textbook used with our MATH 7B course is:

Burger, Edward B., et al. (2015). Texas GoMath! Grade 7. Orlando, FL: Houghton Mifflin Harcourt. ISBN 0-544-10179-0.

Good luck on your examination!

## MATH 7B Key Concepts

| Multiple <br> Representations of Linear Relations | Geometric <br> Relationships | Measurement and Data | Personal Financial Literacy |
| :---: | :---: | :---: | :---: |
| Writing 2-step <br> Equations | Angle Relationships | Analyzing Categorical Data | Calculating Sales and Income Tax |
| Solving 2-step <br> Equations | Finding <br> Circumference <br> Area of Circles | Comparing Data Displayed in Dot Plots | Calculating and Comparing Simple and Compound Interest |
| Solving 2-step Inequalities | Area of Composite Figures | Comparing Data Displayed in Box Plots | Making Purchasing Decisions |
|  | Volume of Rectangular Prisms and Pyramids | Populations and Samples | Personal Budgets |
|  | Volume of Triangular Prisms and Pyramids | Making Inferences from a Random Sample | Planning a Budget <br> Constructing a Net Worth Statement |
|  | Lateral and Total <br> Surface Area | Comparing <br> Populations |  |

## STAAR GRADE 7 MATHEMATICS REFERENCE MATERIALS

## LINEAR EQUATIONS

Slope-intercept form

$$
y=m x+b
$$

Constant of proportionality

$$
k=\frac{y}{x}
$$

## CIRCUMFERENCE

Circle
$C=2 \pi r$
or
$C=\pi d$

## AREA

Triangle
$A=\frac{1}{2} b h$

Rectangle or parallelogram
$A=b h$
Trapezoid $\quad A=\frac{1}{2}\left(b_{1}+b_{2}\right) h$

Circle
$A=\pi r^{2}$

## VOLUME

Prism $\quad V=B h$
Pyramid $\quad V=\frac{1}{3} B h$

ADDITIONAL INFORMATION

| Pi | $\pi \approx 3.14$ | or |
| :--- | :--- | :--- |
| Distance | $d=r t$ |  |
| Simple interest | $I=P r t$ |  |
| Compound interest | $A=P(1+r)^{t}$ |  |

## STAAR GRADE 7 MATHEMATICS REFERENCE MATERIALS

## LENGTH

## Customary

1 mile (mi) $=1,760$ yards $(\mathrm{yd})$
1 yard $(y d)=3$ feet $(f t)$
1 foot (ft) = 12 inches (in.)

Metric
1 kilometer $(\mathrm{km})=1,000$ meters $(\mathrm{m})$
1 meter $(\mathrm{m})=100$ centimeters $(\mathrm{cm})$
1 centimeter $(\mathrm{cm})=10$ millimeters $(\mathrm{mm})$

## VOLUME AND CAPACITY

## Customary

1 gallon (gal) $=4$ quarts (qt)
1 quart (qt) $=2$ pints (pt)
1 pint (pt) $=2$ cups ( c )
1 cup $(c)=8$ fluid ounces (floz)

WEIGHT AND MASS

## Customary

1 ton $(T)=2,000$ pounds ( Ib )
1 pound (lb) = 16 ounces (oz)

Metric
1 liter $(\mathrm{L})=1,000$ milliliters ( mL )

| Length | Weight/Mass | Capacity |
| :--- | :--- | :--- |
| 1 inch $=2.54$ centimeters | 1 ounce $\approx 28.4$ grams | 1 fluid ounce $\approx 29.6$ milliliters |
| 1 foot $\approx 0.305$ meter | 1 pound $\approx 0.454$ kilogram | 1 quart $\approx 0.946$ liter |
| 1 yard $\approx 0.914$ meter |  | 1 gallon $\approx 3.79$ liters |
| 1 mile $\approx 1.61$ kilometers |  |  |

## Texas Essential Knowledge and Skills MATH 7B - Mathematics, Grade 7, Second Semester

| TTU: MATH 7B CBE, v.3.0 |  |
| :---: | :---: |
| TEKS: § 111.25. Mathematics, Grade 7 |  |
| TEKS Requirement (Secondary) | TEKS Covered |
| §111.25. Implementation of Texas Essential Knowledge and Skills for Mathematics, Middle School, Adopted 2012. |  |
| (a) The provisions of $\S \S 111.26-111.28$ of this subchapter shall be implemented by school districts. |  |
| (b) No later than August 31, 2013, the commissioner of education shall determine whether instructional materials funding has been made available to Texas public schools for materials that cover the essential knowledge and skills for mathematics as adopted in $\S \S 111.26-111.28$ of this subchapter. |  |
| (c) If the commissioner makes the determination that instructional materials funding has been made available under subsection (b) of this section, $\S \S 111.26-111.28$ of this subchapter shall be implemented beginning with the 2014-2015 school year and apply to the 2014-2015 and subsequent school years. |  |
| (d) If the commissioner does not make the determination that instructional materials funding has been made available under subsection (b) of this section, the commissioner shall determine no later than August 31 of each subsequent school year whether instructional materials funding has been made available. If the commissioner determines that instructional materials funding has been made available, the commissioner shall notify the State Board of Education and school districts that $\S \S 111.26-111.28$ of this subchapter shall be implemented for the following school year. |  |
| (e) Sections 111.21-111.24 of this subchapter shall be superseded by the implementation of §§111.25-111.28 under this section. |  |
| §111.27. Grade 7, Adopted 2012. |  |
| (a) Introduction. |  |
| (1) The desire to achieve educational excellence is the driving force behind the Texas essential knowledge and skills for mathematics, guided by the college and career readiness standards. By embedding statistics, probability, and finance, while focusing on computational thinking, mathematical fluency, and solid understanding, Texas will lead the way in mathematics education and prepare all Texas students for the challenges they will face in the 21 st century. |  |
| (2) The process standards describe ways in which students are expected to engage in the content. The placement of the process standards at the beginning of the knowledge and skills listed for each grade and course is intentional. The process standards weave the other knowledge and skills together so that students may be successful problem solvers and use mathematics efficiently and effectively in daily life. The process standards are integrated at every grade level and course. When possible, students will apply mathematics to problems arising in everyday life, society, and the workplace. Students will use a problem-solving model that incorporates analyzing given information, formulating a plan or strategy, determining a solution, justifying the solution, and evaluating the problem-solving process and the reasonableness of the solution. Students will select appropriate tools such as real objects, manipulatives, algorithms, paper and pencil, and technology and techniques such as mental math, estimation, number sense, and generalization and abstraction to solve problems. Students will effectively communicate mathematical ideas, reasoning, and their implications using multiple representations such as symbols, diagrams, graphs, computer programs, and language. Students will use mathematical relationships to generate solutions and make connections and predictions. Students will analyze mathematical relationships to connect and communicate mathematical ideas. Students will display, explain, or justify mathematical ideas and arguments using precise mathematical language in written or oral communication. |  |
| (3) The primary focal areas in Grade 7 are number and operations; proportionality; expressions, equations, and relationships; and measurement and data. Students use concepts, algorithms, and properties of rational numbers to explore mathematical relationships and to describe increasingly complex situations. Students use concepts of proportionality to explore, develop, and communicate mathematical relationships, including number, geometry and measurement, and statistics and probability. Students use algebraic thinking to describe how a change in one quantity in a relationship results in a change in the other. Students connect verbal, numeric, graphic, and symbolic representations of relationships, including equations and inequalities. Students use geometric properties and relationships, as well as spatial reasoning, to model and analyze situations and solve problems. Students communicate information about geometric figures or situations by quantifying attributes, generalize procedures from measurement experiences, and use the procedures to solve problems. Students use appropriate statistics, representations of data, and reasoning to draw conclusions, evaluate arguments, and make recommendations. While the use of all types of technology is important, the emphasis on algebra readiness skills necessitates the implementation of graphing technology. |  |


| TTU: MATH 7B CBE, v.3.0 |  |
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| TEKS: § 111.25. Mathematics, Grade 7 |  |
| TEKS Requirement (Secondary) | TEKS Covered |
| (4) Statements that contain the word "including" reference content that must be mastered, while those containing the phrase "such as" are intended as possible illustrative examples. |  |
| (b) Knowledge and skills. |  |
| (1) Mathematical process standards. The student uses mathematical processes to acquire and demonstrate mathematical understanding. The student is expected to: |  |
| (A) apply mathematics to problems arising in everyday life, society, and the workplace; | $\checkmark$ |
| (B) use a problem-solving model that incorporates analyzing given information, formulating a plan or strategy, determining a solution, justifying the solution, and evaluating the problem-solving process and the reasonableness of the solution; | $\checkmark$ |
| (C) select tools, including real objects, manipulatives, paper and pencil, and technology as appropriate, and techniques, including mental math, estimation, and number sense as appropriate, to solve problems; | $\checkmark$ |
| (D) communicate mathematical ideas, reasoning, and their implications using multiple representations, including symbols, diagrams, graphs, and language as appropriate; | $\checkmark$ |
| (E) create and use representations to organize, record, and communicate mathematical ideas; | $\checkmark$ |
| (F) analyze mathematical relationships to connect and communicate mathematical ideas; and | $\checkmark$ |
| (G) display, explain, and justify mathematical ideas and arguments using precise mathematical language in written or oral communication. | $\checkmark$ |
| (2) Number and operations. The student applies mathematical process standards to represent and use rational numbers in a variety of forms. The student is expected to extend previous knowledge of sets and subsets using a visual representation to describe relationships between sets of rational numbers. |  |
| (3) Number and operations. The student applies mathematical process standards to add, subtract, multiply, and divide while solving problems and justifying solutions. The student is expected to: |  |
| (A) add, subtract, multiply, and divide rational numbers fluently; and |  |
| (B) apply and extend previous understandings of operations to solve problems using addition, subtraction, multiplication, and division of rational numbers. |  |
| (4) Proportionality. The student applies mathematical process standards to represent and solve problems involving proportional relationships. The student is expected to: |  |
| (A) represent constant rates of change in mathematical and real-world problems given pictorial, tabular, verbal, numeric, graphical, and algebraic representations, including $\mathrm{d}=\mathrm{rt}$; |  |
| (B) calculate unit rates from rates in mathematical and real-world problems; |  |
| (C) determine the constant of proportionality ( $\mathrm{k}=\mathrm{y} / \mathrm{x}$ ) within mathematical and real-world problems; |  |
| (D) solve problems involving ratios, rates, and percents, including multi-step problems involving percent increase and percent decrease, and financial literacy problems; and |  |
| (E) convert between measurement systems, including the use of proportions and the use of unit rates. |  |
| (5) Proportionality. The student applies mathematical process standards to use geometry to describe or solve problems involving proportional relationships. The student is expected to: |  |
| (A) generalize the critical attributes of similarity, including ratios within and between similar shapes; |  |
| (B) describe $\pi$ as the ratio of the circumference of a circle to its diameter; and |  |
| (C) solve mathematical and real-world problems involving similar shape and scale drawings. |  |
| (6) Proportionality. The student applies mathematical process standards to use probability and statistics to describe or solve problems involving proportional relationships. The student is expected to: |  |
| (A) represent sample spaces for simple and compound events using lists and tree diagrams; |  |
| (B) select and use different simulations to represent simple and compound events with and without technology; |  |
| (C) make predictions and determine solutions using experimental data for simple and compound events; |  |
| (D) make predictions and determine solutions using theoretical probability for simple and compound events; |  |
| (E) find the probabilities of a simple event and its complement and describe the relationship between the two; |  |
| (F) use data from a random sample to make inferences about a population; |  |


| TTU: МАТН 7B CBE, v.3.0 |  |
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| TEKS: § 111.25. Mathematics, Grade 7 |  |
| TEKS Requirement (Secondary) | TEKS Covered |
| (G) solve problems using data represented in bar graphs, dot plots, and circle graphs, including part-to-whole and part-to-part comparisons and equivalents; | $\checkmark$ |
| (H) solve problems using qualitative and quantitative predictions and comparisons from simple experiments; and |  |
| (I) determine experimental and theoretical probabilities related to simple and compound events using data and sample spaces. |  |
| (7) Expressions, equations, and relationships. The student applies mathematical process standards to represent linear relationships using multiple representations. The student is expected to represent linear relationships using verbal descriptions, tables, graphs, and equations that simplify to the form $\mathrm{y}=\mathrm{mx}+\mathrm{b}$. |  |
| (8) Expressions, equations, and relationships. The student applies mathematical process standards to develop geometric relationships with volume. The student is expected to: |  |
| (A) model the relationship between the volume of a rectangular prism and a rectangular pyramid having both congruent bases and heights and connect that relationship to the formulas; |  |
| (B) explain verbally and symbolically the relationship between the volume of a triangular prism and a triangular pyramid having both congruent bases and heights and connect that relationship to the formulas; and |  |
| (C) use models to determine the approximate formulas for the circumference and area of a circle and connect the models to the actual formulas. |  |
| (9) Expressions, equations, and relationships. The student applies mathematical process standards to solve geometric problems. The student is expected to: |  |
| (A) solve problems involving the volume of rectangular prisms, triangular prisms, rectangular pyramids, and triangular pyramids; | $\checkmark$ |
| (B) determine the circumference and area of circles; | $\checkmark$ |
| (C) determine the area of composite figures containing combinations of rectangles, squares, parallelograms, trapezoids, triangles, semicircles, and quarter circles; and | $\checkmark$ |
| (D) solve problems involving the lateral and total surface area of a rectangular prism, rectangular pyramid, triangular prism, and triangular pyramid by determining the area of the shape's net. | $\checkmark$ |
| (10) Expressions, equations, and relationships. The student applies mathematical process standards to use onevariable equations and inequalities to represent situations. The student is expected to: |  |
| (A) write one-variable, two-step equations and inequalities to represent constraints or conditions within problems; | $\checkmark$ |
| (B) represent solutions for one-variable, two-step equations and inequalities on number lines; and | $\checkmark$ |
| (C) write a corresponding real-world problem given a one-variable, two-step equation or inequality. | $\checkmark$ |
| (11) Expressions, equations, and relationships. The student applies mathematical process standards to solve onevariable equations and inequalities. The student is expected to: |  |
| (A) model and solve one-variable, two-step equations and inequalities; | $\checkmark$ |
| (B) determine if the given value(s) make(s) one-variable, two-step equations and inequalities true; and | $\checkmark$ |
| (C) write and solve equations using geometry concepts, including the sum of the angles in a triangle, and angle relationships. | $\checkmark$ |
| (12) Measurement and data. The student applies mathematical process standards to use statistical representations to analyze data. The student is expected to: |  |
| (A) compare two groups of numeric data using comparative dot plots or box plots by comparing their shapes, centers, and spreads; | $\checkmark$ |
| (B) use data from a random sample to make inferences about a population; and | $\checkmark$ |
| (C) compare two populations based on data in random samples from these populations, including informal comparative inferences about differences between the two populations. | $\checkmark$ |
| (13) Personal financial literacy. The student applies mathematical process standards to develop an economic way of thinking and problem solving useful in one's life as a knowledgeable consumer and investor. The student is expected to: |  |


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| :---: | :---: |
| TEKS: § 111.25. Mathematics, Grade 7 |  |
| TEKS Requirement (Secondary) | TEKS Covered |
| (A) calculate the sales tax for a given purchase and calculate income tax for earned wages; | $\checkmark$ |
| (B) identify the components of a personal budget, including income; planned savings for college, retirement, and emergencies; taxes; and fixed and variable expenses, and calculate what percentage each category comprises of the total budget; | $\checkmark$ |
| (C) create and organize a financial assets and liabilities record and construct a net worth statement; | $\checkmark$ |
| (D) use a family budget estimator to determine the minimum household budget and average hourly wage needed for a family to meet its basic needs in the student's city or another large city nearby; | $\checkmark$ |
| (E) calculate and compare simple interest and compound interest earnings; and | $\checkmark$ |
| (F) analyze and compare monetary incentives, including sales, rebates, and coupons. | $\checkmark$ |
| Source: The provisions of this §111.27 adopted to be effective September 10, 2012, 37 TexReg 7109. |  |

