MATH 2300 Final Exam Fall 2018 (175 points possible)

NameR#	
MULTIPLE CHOICE. Choose the one alternative that best completes the state (3 points each)	atement or answers the question.
Provide an appropriate response. 1) Thirty of the 198 students enrolled in Statistics 101 were asked if the take –home or an in–class assessment. Twenty, or about 67%, of the preference for an in–class exam. The professor concluded that the m Statistics 101 would prefer an in–class examination for the second as perform a descriptive study or an inferential study? A) Descriptive B) Inferential	students polled indicated a najority of students in ssessment. Did the professor
Answer the question. 2) In a poll of 50,000 randomly selected college students, 74% answered have a television in your dorm room?" Identify the sample and population of the 50,000 selected college students; population: the 50 Sample: the 74% who answered "yes"; population: all college C) Sample: all college students; population: the 50,000 selected college students; population: all college Sample: the 50,000 selected college students; population: all college students; populati	ulation. 74% who answered "yes" students ollege students
Classify the data as either qualitative or quantitative. 3) The following table shows the average weight of offensive linemen	for each given football team. 3)

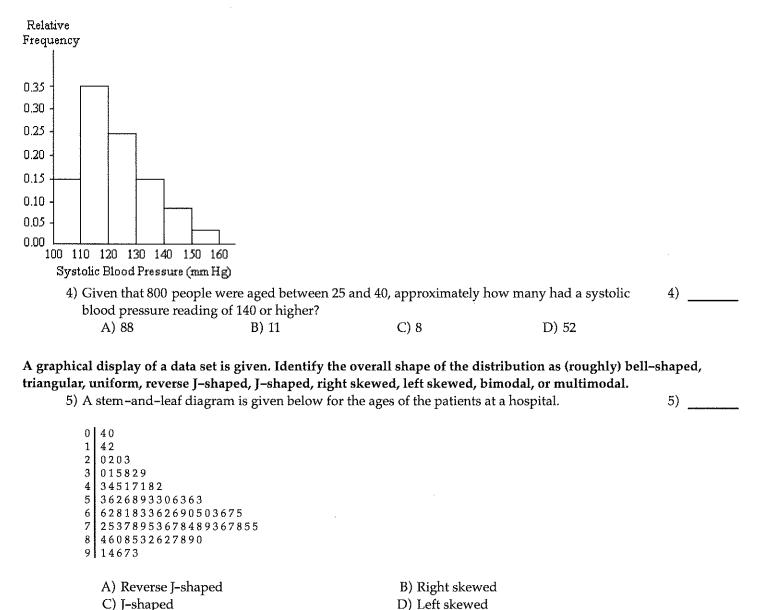
Team	Average weight (pounds)
Gators	303.52
Lakers	326.78
Eagles	290.61
Pioneers	321.96
Lions	297.35
Mustangs	302.49
Rams	345.88
Buffalos	329.24

What kind of data is provided by the information in the first column?

A) Qualitative

B) Quantitative

A nurse measured the blood pressure of each person who visited her clinic. Following is a relative-frequency histogram for the systolic blood pressure readings for those people aged between 25 and 40. Use the histogram to answer the question. The blood pressure readings were given to the nearest whole number.



Construct and interpret a boxplot or a modified boxplot as specified.

6) The normal monthly precipitation (in inches) for August is listed for 20 different U.S. cities. Construct a boxplot for the data.

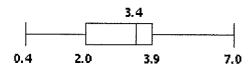
6) _____

0.4 1.0 1.5 1.6 2.0 2.2 2.4 2.7 3.4 3.4

3.5 3.6 3.6 3.7 3.7

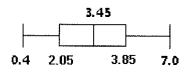
3.9 4.1 4.2 4.2 7.0

A)



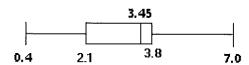
The data is slightly left-skewed.

B)



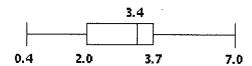
The data is symmetrical. It is a uniform distribution.

C)



The data is slightly left-skewed.

D)

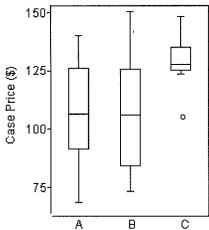


The data is highly left-skewed.

Solve the problem.

7) The boxplots display case prices (in dollars) of white wines produced by three vineyards in the western United States. Describe these wine prices.





A) Vineyards A and B have about the same average price; the boxplots show similar medians and similar IQRs. Vineyard C has consistently higher prices except for one potential outlier, but more variation in pricing as shown by the larger IQR. The distributions for A and B are approximately symmetric, while the distribution for C is right-skewed.

B) Vineyards A and B have different average prices, but a similar variation. Vineyard C has lower prices except for one potential outlier, and less variation in pricing as shown by the smaller IQR. The distributions for A and B are approximately symmetric, while the distribution for C is right-skewed.

C) Vineyards A and B have about the same average price; the boxplots show similar medians and similar IQRs. Vineyard C has higher prices except for one potential outlier, and less variation in pricing as shown by the smaller IQR and overall range. All three distributions are roughly symmetric.

D) Vineyards A and B have about the same average price; the boxplots show similar medians and similar IQRs. Vineyard C has higher prices except for one potential outlier, and a less variation in pricing as shown by the smaller IQR and overall range. Distributions A and B are approximately symmetric, while distribution C is right-skewed.

Find the range for the given data set.

8) Rich Borne is currently taking Chemistry 101. On the five laboratory assignments for the quarter, he got the following scores.

8)	

Estimate the probability of the event.

9) A frequency distribution on employment information from Alpha Corporation follows.. Find the probability that an employee has been with the company 10 years or less.

9)	

Yea	ırs Employed	No. of Employees	l	
	1–5	5	•	
	6-10	10		
	11-15	25		
	16-20	10		
	21-25	5		
	26-30	3		
A) 0.743	I	B) 0.735	C) 0.294	D) 0.259

List the outcomes comprising the specified event.

10) In a competition, two people will be selected from four finalists to receive the first and second prizes. The prize winners will be selected by drawing names from a hat. The names of the four finalists are Jim, George, Helen, and Maggie. The possible outcomes can be represented as follows.

Here, for example, JG represents the outcome that Jim receives the first prize and George receives the second prize. The events A and B are defined as follows.

A = event that Helen gets first prize

B = event that George gets a prize

List the outcomes that comprise the event (A or B).

- A) JG, JH, GJ, GH, GM, HJ, HG, HM, MG, MH
- B) JG, GJ, GH, GM, HJ, HG, HM, MG
- C) HG
- D) JG, GJ, GH, GM, HJ, HM, MG
- 11) Three board members for a nonprofit organization will be selected from a group of five people. The board members will be selected by drawing names from a hat. The names of the five possible board members are Allison, Betty, Charlie, Dave, and Emily. The possible outcomes can be represented as follows.

Here, for example, ABC represents the outcome that Allison, Betty, and Charlie are selected to be on the board. List the outcomes that comprise the following event.

A = event that Betty and Emily are selected

- A) ABC, ABD, ABE, ACE, ADE, BCD, BCE, BDE, CDE
- B) BE
- C) ABE, BCE
- D) ABE, BCE, BDE

Find the indicated probability.

12) A 6-sided die is rolled. What is the probability of rolling a number less than 5?

B) 4

C) $\frac{2}{3}$

D) $\frac{5}{6}$

Find the indicated probability by using the complementation rule.

13) The probability that Luis will pass his statistics test is 0.44. Find the probability that he will fail his statistics test.

13)

12) ____

A) 2.27

B) 0.22

C) 0.56

D) 0.79

Find the specified probability.

14) Use the special addition rule and the following probability distribution to determine $P(6 < X \le 8)$.

14) ____

9 10 P(X = x) = 0.05 = 0.050.20 0.15 0.15 0.10 0.30

A) 0.40

B) 0.35

- C) 0.45
- D) 1.00

Find the mean of the random variable.

15) The random variable X is the number of golf balls ordered by customers at a pro shop. Its probability distribution is given in the table. Round the answer to two decimal places when necessary.

15)

- C) 6.87
- D) 9

Find the indicated probability or percentage for the normally distributed variable.

16) The volumes of soda in quart soda bottles are normally distributed with a mean of 32.3 oz and a standard deviation of 1.2 oz. What is the probability that the volume of soda in a randomly selected bottle will be less than 32 oz?



- A) 0.0987
- B) 0.4013
- C) 0.5987
- D) 0.3821

Find the specified percentile, qu	artile, or decile.			
17) Suppose that replacem	ent times for washing i	nachines are normally dis	stributed with a mean of	17)
		s. Find the 82nd percentil		· <u></u>
A) 9.4 years	B) 10.3 years	C) 8.1 years	D) 9.7 years	
		•		
Provide an appropriate response	2.			
18) True or false, areas und		l curve cannot be negativ	e, whereas z-scores can	18)
be positive or negative			-,	
A) True		B) False		
19) What generally happer	ns to the sampling distr	ribution of the sample me	an as the sample size is	19)
increased?				
A) It is unaffected.				
B) It becomes more	tightly concentrated a	round the population me	an.	•
C) It becomes less t	ightly concentrated arc	ound the population mear	1.	
D) None of the abo	ve			
For samples of the specified size	from the population o	described, find the mean	and standard deviation of	f the sample
mean x.				
20) One barge from Inland that the weights of the	÷	•	ecords of past trips show andard deviation of 16 lb.	20)
For samples of size 64,	find the mean and stan	dard deviation of x.		
A) $\mu_{\bar{x}} = 2$; $\sigma_{\bar{x}} = 94$		B) $\mu_{x} = 94$; σ_{x}	= 16	
C) $\mu_{X} = 16$; $\sigma_{X} = 16$	94	D) $\mu_{x}^{-} = 94$; σ_{x}^{-}	= 2	
Provide an appropriate response				
21) In stating a confidence	-interval estimate of a	population mean, the leve	el of confidence increases	21)
as the size of the interv	al			
A) increases		B) decreases		
Solve the problem.				
22) A confidence interval f of the confidence inter		nas a margin of error of 0.	075. Determine the length	22)
A) 0.038	B) 0.006	C) 0.15	D) 0.075	

Find the confidence interval specified. Assume that the population is normally distributed.

23) A sociologist develops a test to measure attitudes about public transportation, and 27 randomly selected subjects are given the test. Their mean score is 76.2 and their standard deviation is 21.4. Construct the 95% confidence interval for the mean score of all such subjects.

23)

- A) 67.7 to 84.7
- B) 69.2 to 83.2
- C) 64.2 to 88.2
- D) 74.6 to 77.8

A hypothesis test is to be performed. Determine the null and alternative hypotheses.

24) A health insurer has determined that the "reasonable and customary" fee for a certain medical procedure is \$1200. They suspect that the average fee charged by one particular clinic for this procedure is higher than \$1200. The insurer wants to perform a hypothesis test to determine whether their suspicion is correct.



- A) $H_0: \mu > 1200
 - $H_a : \mu = 1200
- C) $H_0: \mu = 1200
 - $H_a: \mu \ge 1200

- B) $H_0: \mu = 1200
- H_a: μ < \$1200 D) H₀: μ = \$1200
 - $H_2: \mu > 1200

For the given hypothesis test, explain the meaning of a Type I error, a Type II error, or a correct decision as specified.

25) A manufacturer claims that the mean amount of juice in its 16 ounce bottles is 16.1 ounces. A consumer advocacy group wants to perform a hypothesis test to determine whether the mean amount is actually less than this. The hypotheses are:

$$H_0: \mu = 16.1 \text{ ounces}$$

 $H_a: \mu < 16.1 \text{ ounces}$

where μ is the mean amount of juice in the manufacturer's 16 ounce bottles. Explain the meaning of a Type I error.

- A) A Type I error would occur if, in fact, μ < 16.1 ounces, but the results of the sampling fail to lead to that conclusion.
- B) A Type I error would occur if, in fact, $\mu = 16.1$ ounces, but the results of the sampling do not lead to rejection of that fact.
- C) A Type I error would occur if, in fact, $\mu = 16.1$ ounces, but the results of the sampling lead to the conclusion that μ < 16.1 ounces.
- D) A Type I error would occur if, in fact, μ < 16.1 ounces, but the results of the sampling lead to the conclusion that $\mu > 16.1$ ounces.

27)

$$H_0: \mu = $1200$$

 $H_a: \mu > 1200

where μ is the mean amount charged by the clinic for this procedure. Explain the meaning of a correct decision.

- A) A correct decision would occur if, in fact, μ > \$1200 and the results of the sampling do not lead to rejection of the null hypothesis that μ = \$1200.
- B) A correct decision would occur if, in fact, μ = \$1200, and the results of the sampling do not lead to rejection of that fact; or if, in fact, μ > \$1200 and the results of the sampling lead to that conclusion.
- C) A correct decision would occur if, in fact, μ = \$1200, and the results of the sampling lead to rejection of the null hypothesis; or if, in fact, μ > \$1200 and the results of the sampling lead to that conclusion.
- D) A correct decision would occur if, in fact, μ = \$1200, and the results of the sampling do not lead to rejection of that fact; or if, in fact, μ > \$1200 and the results of the sampling do not lead to rejection of the null hypothesis that μ = \$1200.
- 27) In the past, the mean running time for a certain type of flashlight battery has been 8.9 hours. The manufacturer has introduced a change in the production method and wants to perform a hypothesis test to determine whether the mean running time has increased as a result. The hypotheses are:

$$H_0: \mu = 8.9 \text{ hours}$$

 $H_a: \mu > 8.9 \text{ hours}$

where $\boldsymbol{\mu}$ is the mean running time of the new batteries . Explain the meaning of a Type II error.

- A) A Type II error would occur if, in fact, μ = 8.9 hours, but the results of the sampling lead to the conclusion that μ > 8.9 hours.
- B) A Type II error would occur if, in fact, μ >8.9 hours, but the results of the sampling fail to lead to that conclusion.
- C) A Type II error would occur if, in fact, $\mu > 8.9$ hours, but the results of the sampling lead to the conclusion that $\mu < 8.9$ hours.
- D) A Type II error would occur if, in fact, μ = 8.9 hours, but the results of the sampling do not lead to rejection of that fact.

Classify the conclusion of the hypothesis test 28) At one school, in 2005, the average a		c, a Type II error, or a correct decision. at tenth-graders spent watching television	28)
-	~	campaign to encourage the students to	
watch less television. One year later,	_		
determine whether the average amo decreased. The hypotheses were:	unt of time spent	watering television per week nad	
$H_0: \mu = 21 \text{ hours}$			
H_a : μ < 21 hours			
where μ is the mean amount of time week.	, in 2006, that ten	th-graders spend watching television each	
conclusion as a Type I error, a Type	II error, or a corre	ejection of the null hypothesis. Classify that ext decision, if in fact the mean amount of	
time, µ, spent watching television ha		0\0	
A) Type I error	B) Type II error	C) Correct decision	
The significance level and P-value of a hypotrejected.	thesis test are giv	en. Decide whether the null hypothesis shou	ıld be
29) $\alpha = 0.10$, P-value = 0.16			29)
A) Reject the null hypothesis.		B) Do not reject the null hypothesis.	
30) $\alpha = 0.05$, P-value = 0.014			30)
A) Reject the null hypothesis.		B) Do not reject the null hypothesis.	
Determine the null and alternative hypothese	es for the propos	ed hypothesis test.	
31) A researcher is interested in determi	ning whether me	n who have completed a postgraduate	31)
degree (master's or Phd) have greate			
		s test to determine whether the mean salary	
a Bachelor's degree only.	raduate degree is	greater than the mean salary of men with	
	of men with a po	ostgraduate degree and let µ2 denote the	
~		nly. The null and alternative hypotheses are	
B) Let x ₁ denote the mean salary	of men with a po	ostgraduate degree and let x2 denote the	
	^	nly. The null and alternative hypotheses are	
$H_0: x_1 = x_2$ and $H_a: x_1 > x_2$.		, 2 1 u u u 1 1 p 0 11.0000 u	
	of men with a po	ostgraduate degree and let µ2 denote the	
•		nly. The null and alternative hypotheses are	
$H_0: \mu_1 > \mu_2 \text{ and } H_a: \mu_1 < \mu_2.$,, F	
D) Let μ_1 denote the mean salary	of men with a po	ostgraduate degree and let μ_2 denote the	

mean salary of men with a Bachelor's degree only. The null and alternative hypotheses are

 $H_0: \mu_1 = \mu_2 \text{ and } H_a: \mu_1 < \mu_2.$

Classify the proposed hypothesis test as Two tailed, Left tailed, or Right tailed.

32) A pharmaceutical company wants to determine whether its new antianxiety medication has any effect on resting pulse rate. They will use a paired sample to determine whether the mean resting pulse rate for adults not taking the antianxiety medication differs from the mean resting pulse rate for adults who are taking the antianxiety medication.

32)

A) Two tailed

B) Left tailed

C) Right tailed

The number of successes and the sample size are given for a simple random sample from a population. Determine the sample proportion, p.

33)
$$x = 33$$
, $n = 40$

33)

- A) p = 0.785
- B) p = 0.825 C) p = 0.725
- D) $\stackrel{\wedge}{p} = 0.835$

Provide an appropriate response.

34) A magazine poll of unemployed men in the U.S. stated "22% of those polled suffer from clinical depression; the margin of error for the poll is plus or minus 6 percentage points." How would you interpret this statement? Assume that the margin of error is associated with a 95% confidence interval.

34)

- A) We can be 95% confident that the percentage of all unemployed men in the U.S. who suffer from clinical depression is somewhere between 16% and 28%.
- B) A confidence interval for the percentage of all unemployed men in the U.S. who suffer from clinical depression is 17% to 27%. There is a 6% chance that this interval does not include the population proportion, p.
- C) The percentage of all unemployed men in the U.S. who suffer from clinical depression is 22%. The chance that this estimate is incorrect is 6%
- D) There is a 95% chance that the percentage of all unemployed men in the U.S. who suffer from clinical depression is somewhere between 16% and 28%.
- 35) A researcher is interested in estimating the proportion of voters who favor a tax on e-commerce. Based on a sample of 250 people, she obtains the following 99% confidence interval for the population proportion p:

35)

$$0.113$$

Which of the statements below is a valid interpretation of this confidence interval?

- A) If 100 different samples of size 250 were selected and, based on each sample, a confidence interval were constructed, exactly 99 of these confidence intervals would contain the true value of p.
- B) If many different samples of size 250 were selected and, based on each sample, a confidence interval were constructed, 99% of the time the true value of p would lie between 0.113 and 0.171
- C) There is a 99% chance that the true value of p lies between 0.113 and 0.171
- D) If many different samples of size 250 were selected and, based on each sample, a confidence interval were constructed, in the long run 99% of the confidence intervals would contain the true value of p.

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

36) Maria constructed the frequency distribution shown below. The data represent the	36)
heights of 60 randomly selected women. (8 points)	

Height	Frequency
54-under 60	7
60-under 61	1
61-under 62	3
62-under 63	5
63-under 64	7
64-under 65	7
65-under 66	6
66-under 72	24

She concluded from her frequency distribution that the heights 66, 67, 68, 69, 70, and 71 inches are the most common for women. What is wrong with her conclusion? How is her frequency distribution misleading and how could the table be improved?

Find the sample mean and sample standard deviation for the given data. Round your final answer to one more decimal place than that used for the observations. (14 points)

37) Christine is currently taking college astronomy. The instructor often gives quizzes. On	37) _	
the past seven quizzes, Christine got the following scores.		

32 17 25 21 20

Find the indicated probability or percentage for the sampling error. (10 points) 38) The amount of coffee that a filling machine puts into an 8 –ounce jar is normally	38)
distributed with a mean of 8.2 ounces and a standard deviation of 0.18 ounce. Determine the percentage of samples of size 16 that will have mean amounts of coffee within 0.1 ounce of the population mean of 8.2 ounces.	
Find the confidence interval specified. (10 points)	
39) A random sample of 88 light bulbs had a mean life of $x = 517$ hours. Assume that $\sigma = 39$ hours. Construct a 90% confidence interval for the mean life, μ , of all light bulbs of this type <u>and</u> determine whether 500 hours would be a plausible value for μ .	39)
Provide an appropriate response. (6 points) 40) Mary wishes to estimate the mean height of women aged 18–24. She picks a sample of	40)
100 women aged between 18 and 24 and constructs a 99% confidence interval for the population mean. If she were to repeat this procedure 200 times in total, she would obtain 200 different confidence intervals. How many of these intervals would you expect to contain the population mean, µ? Explain your thinking.	

Preliminary data analyses indicate that it is reasonable to use a t–test to carry out the specified hypot	hesis test.
(12 points)	

41) A manufacturer makes ball bearings that are supposed to have a mean weight of 30 g. A

retailer suspects that the mean weight is actually less than 30 g. The mean weight for a
random sample of 16 ball bearings is 28.6 g with a standard deviation of 4.4 g. At the 5%
significance level, test the claim that the mean is less than 30 g.

Provide an appropriate response.

42) Suppose that you wish to perform a hypothesis test for a population mean using the critical value method. The test is right-tailed. Suppose that the population standard deviation is unknown. The correct procedure to use is the t-test. If you mistakenly use the standard normal table to obtain the critical value, will the value that you obtain be larger or smaller than the correct value? Does the mistaken use of the normal table make it more or less likely that the null hypothesis will be rejected?

42)	