

**To the Student:**

After your registration is complete and your proctor has been approved, you may take the Credit by Examination for PRE CALC 1B.

**WHAT TO BRING**

- several sharpened No. 2 pencils
- graphing calculator
- extra sheets of scratch paper

**ABOUT THE EXAM**

The examination for the second semester of Precalculus consists of 28-29 questions. The exam is based on the Texas Essential Knowledge and Skills (TEKS) for this subject. The full list of TEKS is included in this document (it is also available online at the Texas Education Agency website, <http://www.tea.state.tx.us/>). The TEKS outline specific topics covered in the exam, as well as more general areas of knowledge and levels of critical thinking. Use the TEKS to focus your study in preparation for the exam.

The examination will take place under supervision, and the recommended time limit is three hours. You may not use any notes or books. You may use a graphing calculator on this exam, but in order to receive credit for a problem, you must show all of your work and label your graphs. When possible, exact answers should be given. Numerical approximations involving decimals will NOT be accepted for exact answers. (For example: 0.8660 will not be accepted for  $\frac{\sqrt{3}}{2}$ .) If an exact answer is not possible, write decimal approximations to three decimal places unless otherwise noted. You will write your answers on the exam.

A percentage score from the examination will be reported to the official at your school.

In preparation for the examination, review the TEKS for this subject. All TEKS are assessed. It is important to prepare adequately. Since questions are not taken from any one source, you can prepare by reviewing any of the state-adopted textbooks that are used at your school.

To help you better prepare for the exam, a practice exam has been provided. It is **not** a duplicate of the actual examination. It is provided to illustrate the format of the exam, not to serve as a complete review sheet. Follow the instructions on the practice exam so that you will know what is expected of you when you take the real exam.

Good luck on your examination!

## PRE CALC 1B Formula Chart

$$\omega = \frac{\theta}{t}$$

$$v = \frac{s}{t}$$

$$v = r \omega$$

$$x = r \cos \theta$$

$$y = r \sin \theta$$

$$x = (v_0 \cos \theta)t$$

$$y = (v_0 \sin \theta)t - 16t^2 + h_0$$

$$y = (v_0 \sin \theta)t - 4.9t^2 + h_0$$

$$\sin(u + v) = \sin u \cos v + \cos u \sin v$$

$$\sin(u - v) = \sin u \cos v - \cos u \sin v$$

$$\cos(u + v) = \cos u \cos v - \sin u \sin v$$

$$\cos(u - v) = \cos u \cos v + \sin u \sin v$$

$$\tan(u + v) = \frac{\tan u + \tan v}{1 - \tan u \tan v}$$

$$\tan(u - v) = \frac{\tan u - \tan v}{1 + \tan u \tan v}$$

$$\sin 2u = 2 \sin u \cos u$$

$$\cos 2u = \cos^2 u - \sin^2 u$$

$$\tan 2u = \frac{2 \tan u}{1 - \tan^2 u}$$

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$$

$$\frac{(x-h)^2}{a^2} - \frac{(y-k)^2}{b^2} = 1$$

$$y = a(x-h)^2 + k$$

$$x = a(y-k)^2 + h$$

## PRE CALC 1B Practice Exam

**Directions:** Take this exam without reference to any books or notes, exactly as you will during the actual exam. You may use a graphing calculator on the exam, but in order to receive credit for a problem, you must show all of your work and label your graphs. Numerical approximations involving decimals should be written to three decimal places unless otherwise noted. When possible exact answers should be given. (For example: 0.8660 will not be accepted for  $\frac{\sqrt{3}}{2}$ .) Write your answers on this exam.

Check your answers with the answer key provided.

1. Point P with coordinates  $(-1, 3)$  is on the terminal side of  $\theta$ , an angle in standard position. Find the *exact* values of the six trigonometric functions of  $\theta$ .

$$\sin \theta =$$

$$\cos \theta =$$

$$\tan \theta =$$

$$\csc \theta =$$

$$\sec \theta =$$

$$\cot \theta =$$

*continued*  $\rightarrow$

2. Express  $\frac{2\pi}{9}$  in degrees.

3. If  $\sin \theta = \frac{\sqrt{2}}{2}$  and  $\theta$  is in quadrant II, find the *exact* value of  $\cos \theta$ .

4. Find the *exact* value of each of the following:

A.  $\sin \frac{5\pi}{3}$

B.  $\cos 180^\circ$

C.  $\tan \frac{3\pi}{4}$

*continued*  $\rightarrow$

5. Find the angular velocity, in radians per minute, of an object rotating at 150 revolutions per minute.

6. Solve for  $0 \leq \theta < 2\pi$ . (*exact solutions*)  $2 \sin^2 \theta - \sin \theta - 1 = 0$ .

7. You are standing 50 meters from the base of the Empire State Building. You estimate that the angle of elevation to the top of the observation deck is  $80^\circ$ . If the total height of the building is 123 meters above the observatory, find the approximate height of the building.

*continued*  $\rightarrow$

8. Determine the following for the given function:  $y = 2 \cos 2\left(x - \frac{\pi}{2}\right) + 1$

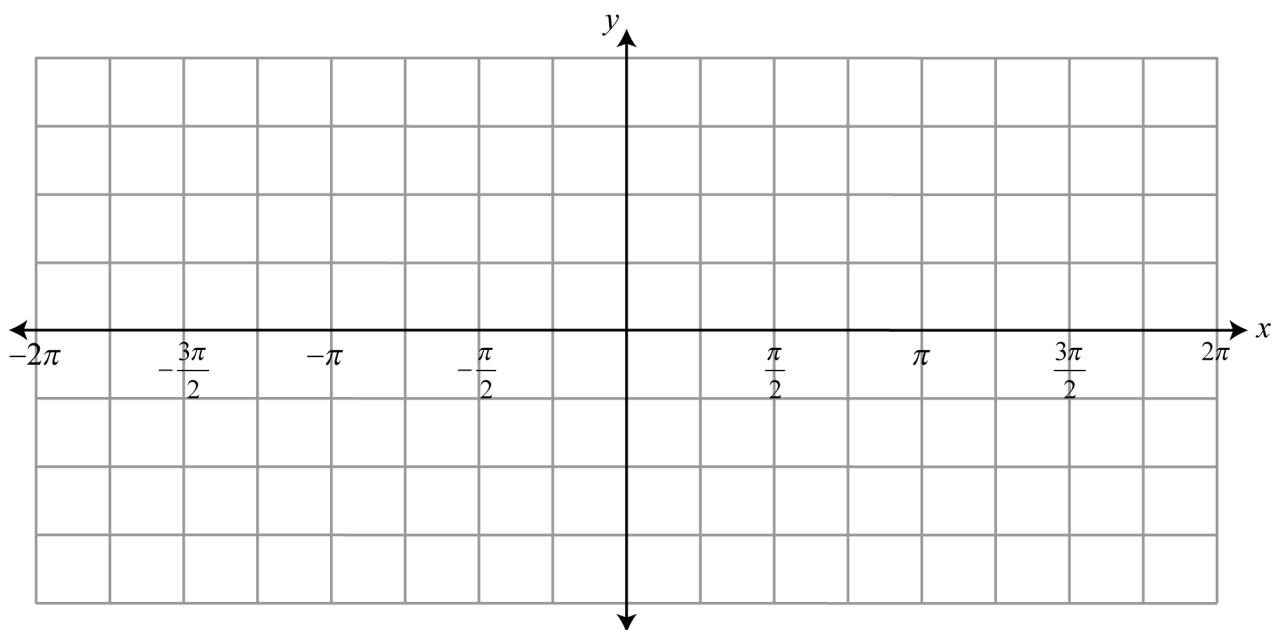
A. amplitude = \_\_\_\_\_

B. period = \_\_\_\_\_

C. phase shift = \_\_\_\_\_

D. vertical shift = \_\_\_\_\_

E. Graph on the interval  $[-2\pi, 2\pi]$ .



*continued* →

9. The normal monthly temperatures in degrees Fahrenheit for six months for a certain northern city are listed in the table below.

$x$ (month)	$y$ (temperature)
Jan	21
Mar	34
May	58
Jul	72
Sep	61
Nov	40

- A. Write a trigonometric function to model this data and sketch its graph.

- B. Use the trig model to find the normal temperature in December.

*continued* →

10. Solve  $\triangle XYZ$  if  $\angle X = 24^\circ$ ,  $\angle Z = 48^\circ$ , and  $y = 27.5$ .
11. Solve  $\triangle CHS$  if  $c = 75$ ,  $h = 50$ , and  $s = 110$ . Round angle measures to the nearest degree.
12. An airplane has an air speed of 500 km per hour at a bearing of  $30^\circ$ . The wind velocity is 50 km per hour in the direction of N  $60^\circ$  E. Find the resultant speed and direction of the airplane.

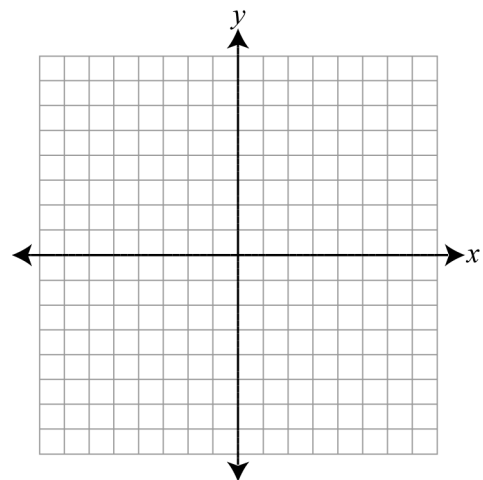
*continued*  $\rightarrow$



13. Given  $A(-2, 1)$  and  $B(4, 5)$ , write the component form of  $\overrightarrow{AB}$  and then find its magnitude and direction.

14. Let  $\mathbf{u} = \langle -2, -3 \rangle$  and  $\mathbf{v} = \langle 6, 4 \rangle$ .

- A. Find  $\mathbf{u} + \mathbf{v}$  algebraically and then verify by geometrically showing the sum on the graph.



- B. Find  $2\mathbf{u} - \mathbf{v}$ .

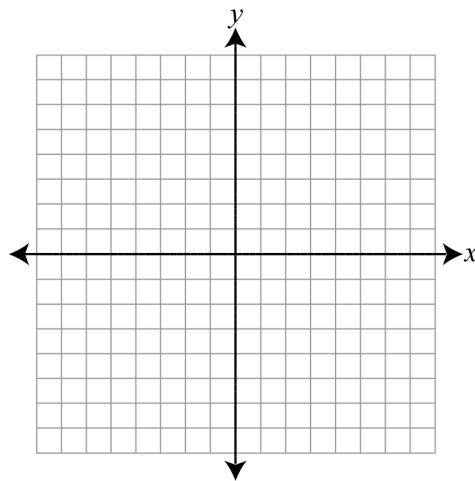
*continued*  $\rightarrow$

15. A football is kicked with an initial velocity of 85 feet per second at an angle of  $40^\circ$  with the horizontal. Find the vertical and horizontal components of the velocity vector to three decimal places.
16. An airplane has an air speed of 650 kilometers per hour at a bearing of  $120^\circ$ . The wind velocity is 25 kilometers per hour from the east. Use vectors to find the resultant speed and direction of the airplane.

*continued*  $\rightarrow$

17. Write the parametric equations in rectangular form. Then graph.

$$\begin{aligned}x &= 2 - t \\ y &= t^2 - 4t + 6\end{aligned}$$



18. A quarterback releases a pass at a height of 7 feet above the playing field. The pass is released at an angle of  $35^\circ$  with an initial velocity of 54 ft/s.

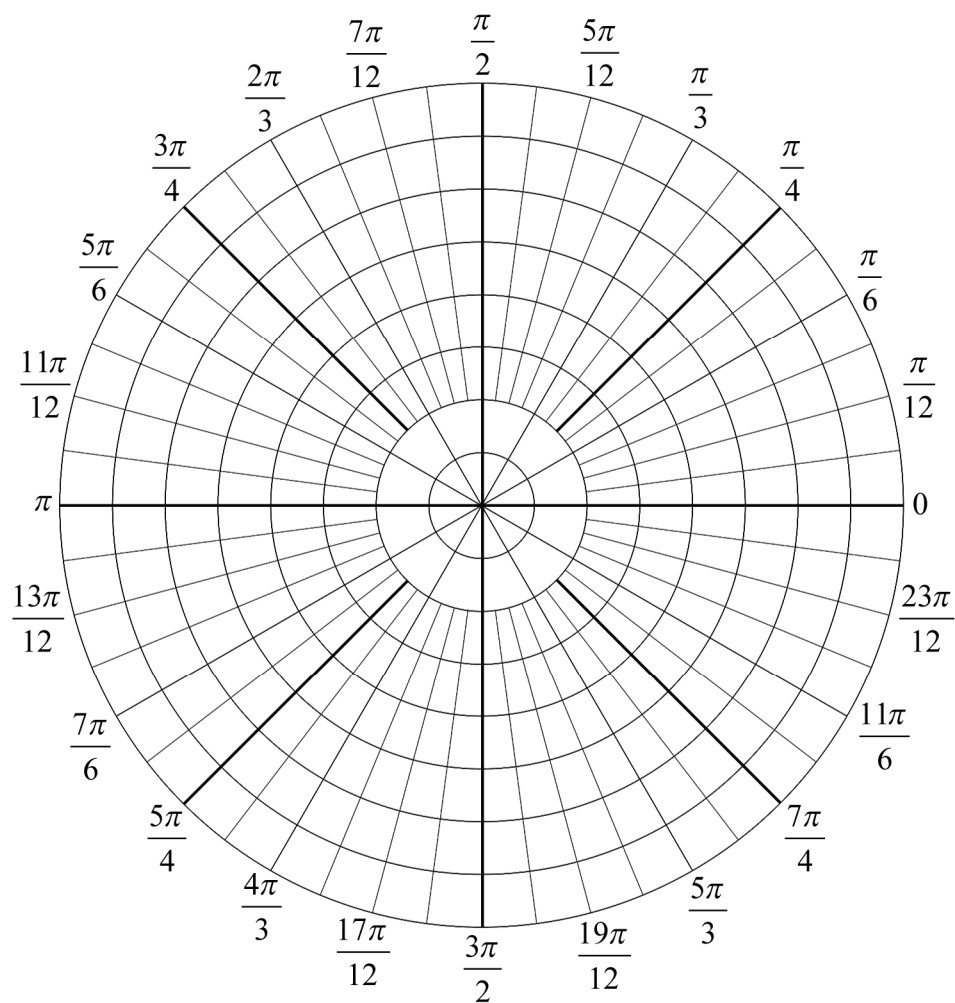
A. Write a set of parametric equations to model the path of the baseball.

B. If the receiver misses the pass, how long is the ball in the air?

C. How far does the ball travel horizontally?

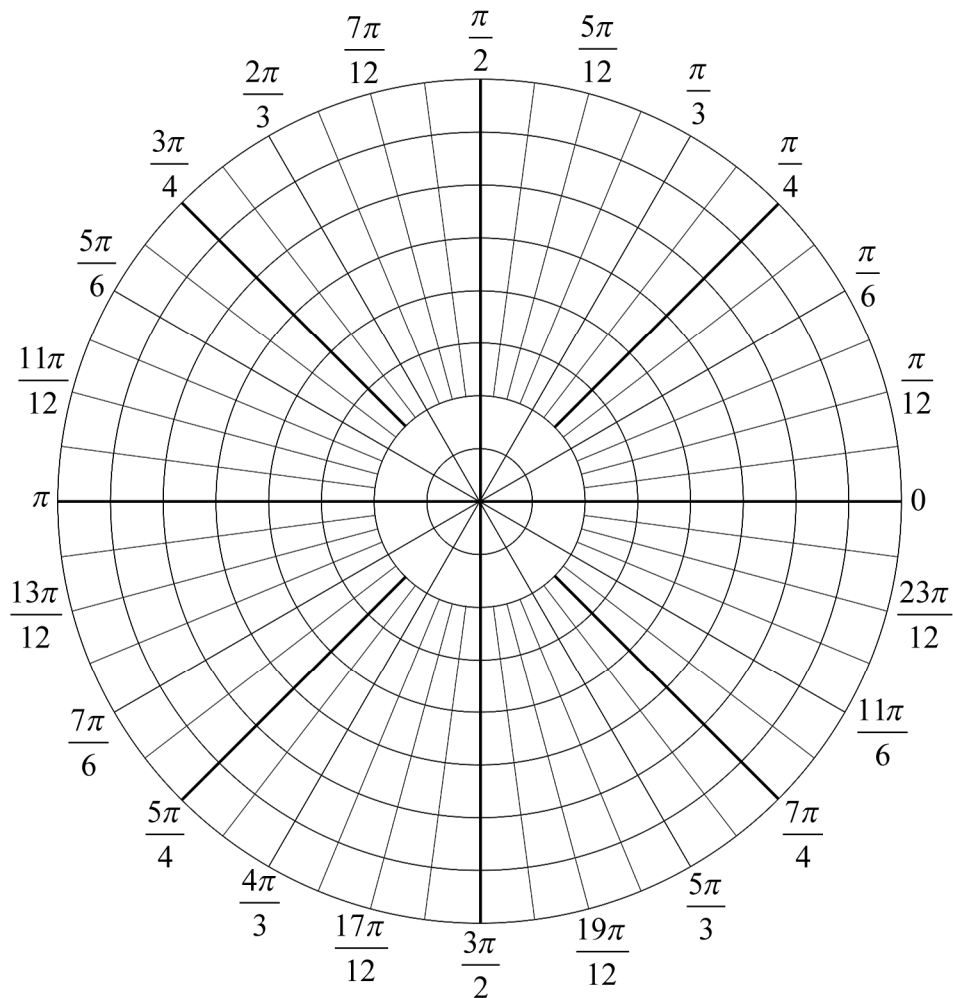
*continued*  $\rightarrow$

19. Plot the polar coordinate  $\left(-2, \frac{7\pi}{6}\right)$  and then convert the coordinate to rectangular form using *exact* solutions.



*continued* →

20. Identify the equation and then graph the polar equation:  $r = 2 - 2 \sin \theta$ .



21. Identify the conic section represented by:  $5x^2 - 2y^2 + 10x - 4y + 17 = 0$ .

*continued* →

22. Write the equation for an ellipse with vertices  $(4, 3)$  and  $(4, 7)$  and foci at  $(4, 4)$  and  $(4, 6)$ .

23. Write the equation for a hyperbola with vertices  $(3, 3)$  and  $(-3, 3)$  and foci  $(4, 3)$  and  $(-4, 3)$ .

24. Write an equation for a set of points that are equidistant from the line  $x = 4$  and the point  $(-2, 0)$ .

*continued*  $\rightarrow$

25. Use trigonometric identities to simplify each expression in terms of one trig function.

A.  $\frac{\csc^2 \theta - \cot^2 \theta}{\tan^2 \theta \csc^2 \theta}$

B.  $(\tan^2 x + 1)(\cos^2 x - 1)$

26. Use an identity to verify:  $\sin\left(\frac{\pi}{2} + x\right) = \cos x$ .

*continued*  $\rightarrow$

27. Solve on  $(0, 2\pi]$  (*exact solutions*)  $2\sec^2 x + \tan^2 x - 3 = 0$ .

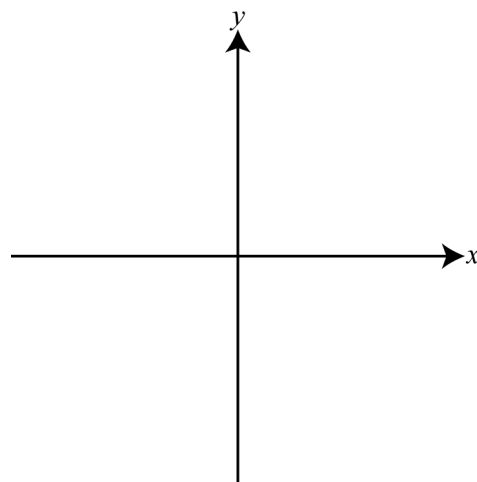
28. Graph  $y = \arctan x$  and answer the questions below.

A. domain =

B. range =

C. Is the function even or odd?

Describe its symmetry.





## PRE CALC 1B Practice Exam Answer Key

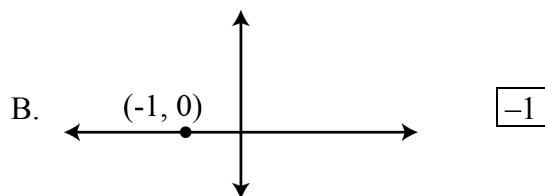
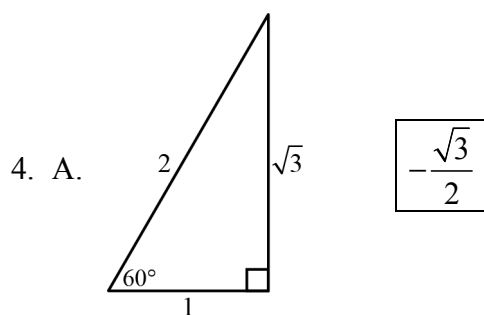
$$1. \quad \sin \theta = \frac{3}{\sqrt{10}} = \boxed{\frac{3\sqrt{10}}{10}} \quad \csc \theta = \boxed{\frac{\sqrt{10}}{3}}$$

$$\cos \theta = \frac{-1}{\sqrt{10}} = \boxed{-\frac{\sqrt{10}}{10}} \quad \sec \theta = \boxed{-\sqrt{10}}$$

$$\tan \theta = \frac{3}{-1} = \boxed{-3} \quad \cot \theta = \boxed{-\frac{1}{3}}$$

$$2. \quad \frac{2\pi}{9} \cdot \frac{180}{\pi} = \boxed{40^\circ}$$

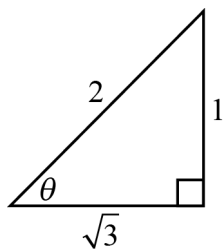
$$3. \quad -\frac{\sqrt{2}}{2}$$



C.  $\boxed{-1}$

$$5. \quad \frac{150 \text{ rev}}{\text{min}} \left| \frac{2\pi}{1 \text{ rev}} \right. = \boxed{300 \pi \text{ rad/min}} \text{ or } 942.478 \text{ rad/min}$$

6.  $2 \sin^2 \theta - \sin \theta - 1 = 0$



ref  $\angle = \frac{\pi}{6}$

$$\sin \theta = -\frac{1}{2}$$

$$\text{III: } \pi + \frac{\pi}{6} = \frac{7\pi}{6}$$

$$\text{IV: } 2\pi - \frac{\pi}{6} = \frac{11\pi}{6}$$

$$(2 \sin \theta + 1)(\sin \theta - 1) = 0$$

$$2 \sin \theta = -1 \quad \sin \theta = 1$$

$$\sin \theta = -\frac{1}{2} \quad \sin \theta = \frac{\pi}{2}$$

$$\theta = \boxed{\frac{7\pi}{6}, \frac{11\pi}{6}, \frac{\pi}{2}}$$

7.  $\tan 80^\circ = \frac{h}{50}$

$$50(\tan 80^\circ) = h$$

$$283.564 = h$$

$$283.564$$

building: +123

$$\boxed{406.564 \text{ m}}$$

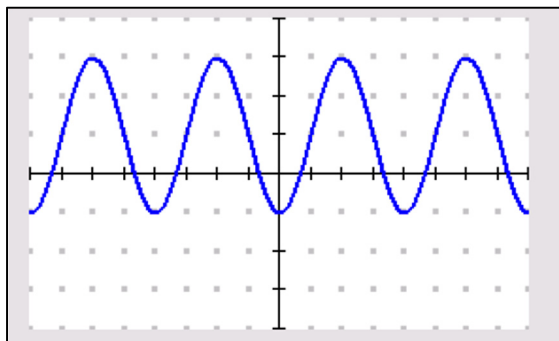
8. A. amplitude = 2

B. period =  $\pi$

C. phase shift =  $\frac{\pi}{2}$

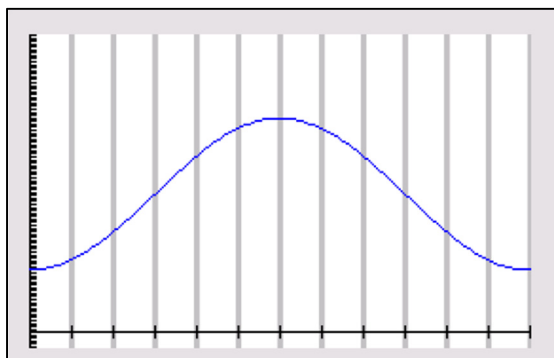
D. vertical shift = 1

E.



(Note: each space on the x-axis =  $\frac{\pi}{4}$ ; each space on the y-axis = 1.)

9. A.



per = 12 mo.      vert. shift =  $21 + 25.5 = 46.5$

$$\frac{2\pi}{b} = 12$$

horiz. shift = 6

$$b = \frac{\pi}{6}$$

$$y = 25.5 \cos \frac{\pi}{6}(t - 6) + 46.5$$

$$\begin{aligned} \text{amp} &= \frac{72 - 21}{2} \\ &= 25.5 \end{aligned}$$

B.  $y = 25.5 \cos \frac{\pi}{6}(11 - 6) + 46.5$   
 $= 24.416$   
 $\approx 24^\circ$

December temperature is approximately  $24^\circ$ .  
 $t = 0$  is January.

10.  $\angle Y = 108^\circ$

$$\frac{\sin 108^\circ}{27.5} = \frac{\sin 24^\circ}{x}$$

$$x = 11.761$$

$$\frac{\sin 108^\circ}{27.5} = \frac{\sin 48^\circ}{z}$$

$$z = 21.488$$

11.  $\cos \angle C = \frac{75^2 - 50^2 - 110^2}{-2(50)(110)}$

$$\angle C = 35.323^\circ$$

$$\angle C \approx 35^\circ$$

$$\cos \angle H = \frac{50^2 - 110^2 - 75^2}{-2(110)(75)}$$

$$\angle H = 22.672^\circ$$

$$\angle H \approx 23^\circ$$

$$\angle S \approx 122^\circ$$

$$12. \text{ resultant speed} = \sqrt{500^2 + 50^2 - 2(500)(50)\cos 150^\circ}$$

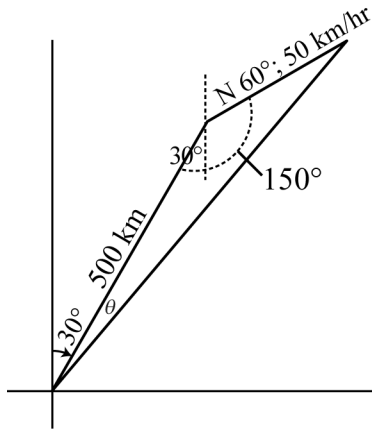
$$= \boxed{543.876 \text{ km/h}}$$

$$\frac{\sin \theta}{50} = \frac{\sin 150^\circ}{543.876}$$

$$\theta = 2.635^\circ$$

$$\text{bearing} = 30^\circ + \theta$$

$$= \boxed{32.635^\circ}$$



$$13. \quad \overrightarrow{AB} = \langle 6, 4 \rangle$$

$$|\overrightarrow{AB}| = \sqrt{6^2 + 4^2}$$

$$= \sqrt{36 + 16}$$

$$= \sqrt{52}$$

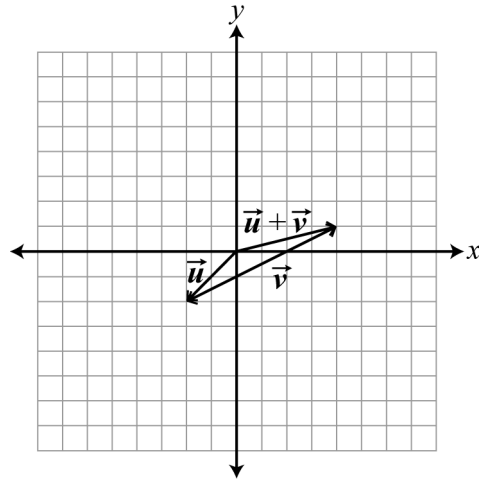
$$= \boxed{2\sqrt{13} \approx 7.211}$$

$$\text{direction} = \tan \theta = \frac{4}{6} = \boxed{33.690^\circ}$$

*continued* →

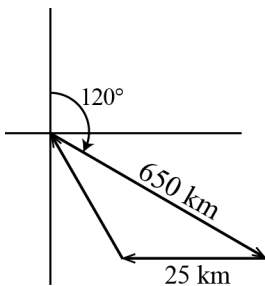
14. A.  $\vec{u} + \vec{v} = \langle -2, -3 \rangle + \langle 6, 4 \rangle$   
 $= \langle 4, 1 \rangle$

B.  $2\vec{u} - \vec{v} = 2\langle -2, -3 \rangle - \langle 6, 4 \rangle$   
 $\langle -4, -6 \rangle - \langle 6, 4 \rangle$   
 $\langle -10, -10 \rangle$



15. horizontal component:  $x = (85 \cos 40^\circ) \approx \boxed{65.114}$   
vertical component:  $y = (85 \sin 40^\circ) \approx \boxed{54.637}$

16. plane =  $\langle 650 \cos -30^\circ, 650 \sin -30^\circ \rangle$   
 $= \langle 562.917, -325 \rangle$   
wind =  $\langle -25, 0 \rangle$



Bearing of  $120^\circ$  = direction angle of  $-30^\circ$  or  $330^\circ$

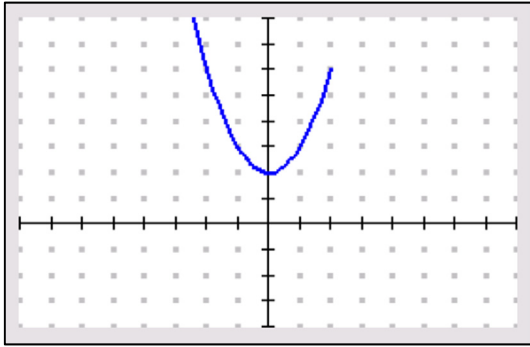
resultant vector =  $\langle 537.917, -325 \rangle$ ; speed =  $\boxed{628.474 \text{ km/h}}$

direction angle =  $\boxed{-31.140^\circ}$  which is a bearing of  $121.140^\circ$

*continued*  $\rightarrow$

17.  $x = 2 - t$   
 $t = 2 - x$

$$\begin{aligned} y &= t^2 - 4t + 6 \\ &= (2-x)^2 - 4(2-x) + 6 \\ &= 4 = \cancel{4x} + x^2 - 8 + \cancel{4x} + 6 \\ y &= \boxed{x^2 + 2} \end{aligned}$$



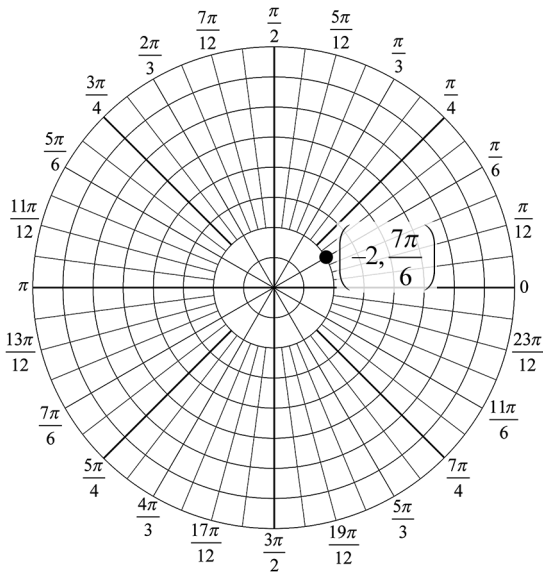
$t$	$x$	$y$
0	2	6
1	1	3
2	0	2
3	-1	3
4	-2	6

18. A.  $x = (54 \cos 35^\circ)t$   
 $y = (54 \sin 35^\circ)t - 16t^2 + 7$

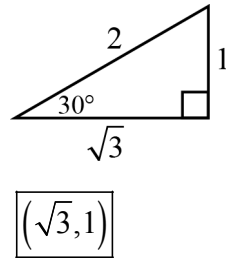
B.  $-16t^2 + (54 \sin 35^\circ)t + 7 = 0$   
 $t \approx \cancel{-0.2044}$  or  $\boxed{2.1402 \text{ seconds}}$

C.  $x = (54 \cos 35^\circ)(2.1402)$   
 $= \boxed{94.6701 \text{ feet}}$

19.



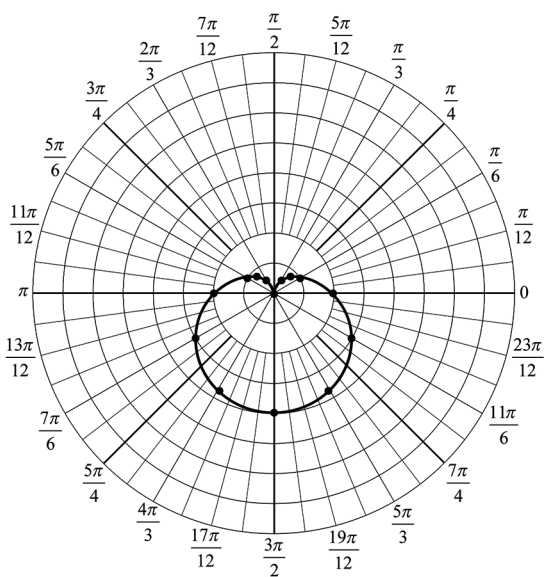
$$\begin{aligned} x &= r \cos \theta \\ &= -2 \cos \frac{7\pi}{6} \\ &= -2 \left( -\frac{\sqrt{3}}{2} \right) \\ &= \sqrt{3} \end{aligned}$$



$$\begin{aligned} y &= r \sin \theta \\ &= -2 \cos \frac{7\pi}{6} \\ &= -2 \left( -\frac{1}{2} \right) \\ &= 1 \end{aligned}$$

20. Cardioid: symmetric to  $\theta = \frac{\pi}{2}$

$\theta$	$r$
0	2
$\frac{\pi}{6}$	1
$\frac{\pi}{4}$	.586
$\frac{\pi}{3}$	.268
$\frac{\pi}{2}$	0
$\frac{3\pi}{2}$	4
$\frac{5\pi}{3}$	3.732
$\frac{11\pi}{6}$	3



21. hyperbola

22. center (4, 5)

$$c^2 = a^2 - b^2$$

$$1 = 4 - b^2$$

$$b^2 = 3$$

$$\frac{(x-4)^2}{3} - \frac{(y-5)^2}{4} = 1$$

*continued* →

23. center (0, 3)

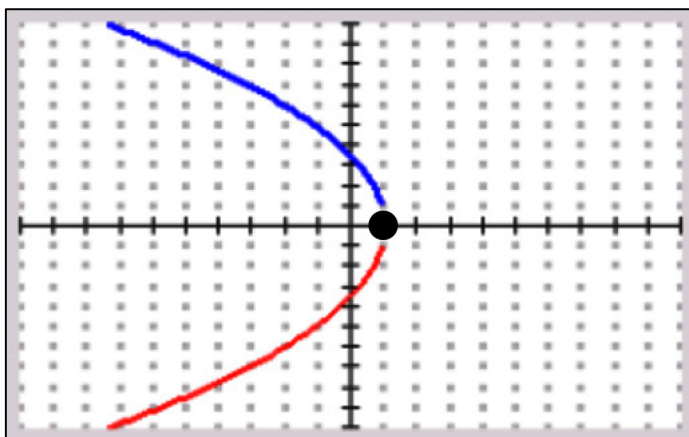
$$c^2 = a^2 + b^2$$

$$16 = 9 + b^2$$

$$7 = b^2$$

$$\frac{x^2}{9} - \frac{(y-3)^2}{7} = 1$$

24. A **parabola** is the conic section in which all points are equidistant from a given point called the focus and a given line called the directrix.



vertex (1, 0)

$$p = -3$$

$$a = \frac{1}{4(-3)}$$

$$= -\frac{1}{12}$$

Parabola:

$$x = a(y - k)^2 + h$$

$$x = -\frac{1}{12}y^2 + 1$$

*continued* →



$$\begin{aligned}
 25. \quad A. \quad & \frac{\csc^2 \theta - \cot^2 \theta}{\tan^2 \theta \csc^2 \theta} \\
 &= \frac{1}{\frac{\cancel{\sin^2 \theta}}{\cos^2 \theta} \cdot \frac{1}{\cancel{\sin^2 \theta}}} \\
 &= \frac{1}{\sec^2 \theta} \\
 &= \cos^2 \theta
 \end{aligned}$$

$$\begin{aligned}
 B. \quad & (\tan^2 x + 1)(\cos^2 x - 1) \\
 & \tan^2 x \cos^2 x - \tan^2 x + \cos^2 x - 1 \\
 & \frac{\cancel{\sin^2 x}}{\cancel{\cos^2 x}} \cdot \cancel{\cos^2 x} - \tan^2 x + \cos^2 x - 1 \\
 & (\sin^2 x + \cos^2 x) - 1 - \tan^2 x \\
 & 1 - 1 - \tan^2 x \\
 & -\tan^2 x
 \end{aligned}$$

$$\begin{aligned}
 26. \quad & \sin\left(\frac{\pi}{2} + x\right) = \cos x \\
 & \sin \frac{\pi}{2} \cos x + \cos \frac{\pi}{2} \sin x \\
 & 1 (\cos x) + 0 (\sin x) \\
 & \cos x + 0 \\
 & \cos x \checkmark
 \end{aligned}$$

$$27. \quad 1 + \tan^2 x = \sec^2 x \qquad 2(1 + \tan^2 x) + \tan^2 x - 3 = 0$$

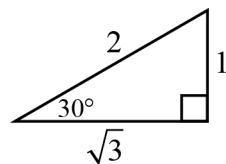
$$2 + 2 \tan^2 x + \tan^2 x - 3 = 0$$

$$3 \tan^2 x - 1 = 0$$

$$3 \tan^2 x = 1$$

$$\tan^2 x = \frac{1}{3}$$

$$\tan x = \pm \frac{1}{\sqrt{3}}$$

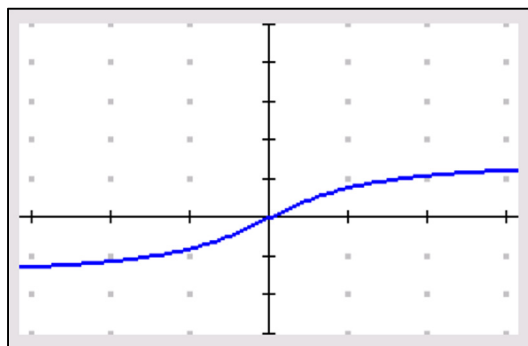


$\frac{\pi}{6}$	$\frac{5\pi}{6}$	$\frac{7\pi}{6}$	$\frac{11\pi}{6}$
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28. A. domain:  $(-\infty, \infty)$

B. range:  $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$

C. odd; origin symmetry



# Texas Essential Knowledge and Skills PRE CALC 1B – Precalculus, Second Semester

TTU: PRE CALC 1B CBE, v.3.0	
TEKS: §111.42. Precalculus, Adopted 2012 (One-Half Credit)	
TEKS Covered	TEKS Covered
	<b>§111.38. Implementation of Texas Essential Knowledge and Skills for Mathematics, High School, Adopted 2012.</b>
	(a) The provisions of §§111.39-111.45 of this subchapter shall be implemented by school districts.
	(b) No later than June 30, 2015, the commissioner of education shall determine whether instructional materials funding has been made available to Texas public schools for materials that cover the essential knowledge and skills for mathematics as adopted in §§111.39-111.45 of this subchapter.
	(c) If the commissioner makes the determination that instructional materials funding has been made available under subsection (b) of this section, §§111.39-111.45 of this subchapter shall be implemented beginning with the 2015-2016 school year and apply to the 2015-2016 and subsequent school years.
	(d) If the commissioner does not make the determination that instructional materials funding has been made available under subsection (b) of this section, the commissioner shall determine no later than June 30 of each subsequent school year whether instructional materials funding has been made available. If the commissioner determines that instructional materials funding has been made available, the commissioner shall notify the State Board of Education and school districts that §§111.39-111.45 of this subchapter shall be implemented for the following school year.
	(e) Sections 111.31-111.37 of this subchapter shall be superseded by the implementation of §§111.38-111.45 under this section.
	<i>Source: The provisions of this §111.38 adopted to be effective September 10, 2012, 37 TexReg 7109.</i>
	<b>§111.42. Precalculus, Adopted 2012.</b>
	(a) General requirements. Students shall be awarded one-half to one credit for successful completion of this course. Prerequisites: Algebra I, Geometry, and Algebra II.
	(b) Introduction.
	(1) The desire to achieve educational excellence is the driving force behind the Texas essential knowledge and skills for mathematics, guided by the college and career readiness standards. By embedding statistics, probability, and finance, while focusing on fluency and solid understanding, Texas will lead the way in mathematics education and prepare all Texas students for the challenges they will face in the 21st century.
	(2) The process standards describe ways in which students are expected to engage in the content. The placement of the process standards at the beginning of the knowledge and skills listed for each grade and course is intentional. The process standards weave the other knowledge and skills together so that students may be successful problem solvers and use mathematics efficiently and effectively in daily life. The process standards are integrated at every grade level and course. When possible, students will apply mathematics to problems arising in everyday life, society, and the workplace. Students will use a problem-solving model that incorporates analyzing given information, formulating a plan or strategy, determining a solution, justifying the solution, and evaluating the problem-solving process and the reasonableness of the solution. Students will select appropriate tools such as real objects, manipulatives, paper and pencil, and technology and techniques such as mental math, estimation, and number sense to solve problems. Students will effectively communicate mathematical ideas, reasoning, and their implications using multiple representations such as symbols, diagrams, graphs, and language. Students will use mathematical relationships to generate solutions and make connections and predictions. Students will analyze mathematical relationships to connect and communicate mathematical ideas. Students will display, explain, or justify mathematical ideas and arguments using precise mathematical language in written or oral communication.
	(3) Precalculus is the preparation for calculus. The course approaches topics from a function point of view, where appropriate, and is designed to strengthen and enhance conceptual understanding and mathematical reasoning used when modeling and solving mathematical and real-world problems. Students systematically work with functions and their multiple representations. The study of Precalculus deepens students' mathematical understanding and fluency with algebra and trigonometry and extends their ability to make connections and apply concepts and procedures at higher levels. Students investigate and explore mathematical ideas, develop multiple strategies for analyzing complex situations, and use technology to build understanding, make connections between representations, and provide support in solving problems.
	(4) Statements that contain the word "including" reference content that must be mastered, while those containing the phrase "such as" are intended as possible illustrative examples.
	(c) Knowledge and skills.

	<b>(1) Mathematical process standards.</b> The student uses mathematical processes to acquire and demonstrate mathematical understanding. The student is expected to:
✓	(A) apply mathematics to problems arising in everyday life, society, and the workplace;
✓	(B) use a problem-solving model that incorporates analyzing given information, formulating a plan or strategy, determining a solution, justifying the solution, and evaluating the problem-solving process and the reasonableness of the solution;
✓	(C) select tools, including real objects, manipulatives, paper and pencil, and technology as appropriate, and techniques, including mental math, estimation, and number sense as appropriate, to solve problems;
✓	(D) communicate mathematical ideas, reasoning, and their implications using multiple representations, including symbols, diagrams, graphs, and language as appropriate;
✓	(E) create and use representations to organize, record, and communicate mathematical ideas;
✓	(F) analyze mathematical relationships to connect and communicate mathematical ideas; and
✓	(G) display, explain, and justify mathematical ideas and arguments using precise mathematical language in written or oral communication.
	<b>(2) Functions.</b> The student uses process standards in mathematics to explore, describe, and analyze the attributes of functions. The student makes connections between multiple representations of functions and algebraically constructs new functions. The student analyzes and uses functions to model real-world problems. The student is expected to:
	(A) use the composition of two functions to model and solve real-world problems;
	(B) demonstrate that function composition is not always commutative;
	(C) represent a given function as a composite function of two or more functions;
✓	(D) describe symmetry of graphs of even and odd functions;
	(E) determine an inverse function, when it exists, for a given function over its domain or a subset of its domain and represent the inverse using multiple representations;
✓	(F) graph exponential, logarithmic, rational, polynomial, power, trigonometric, inverse trigonometric, and piecewise defined functions, including step functions;
✓	(G) graph functions, including exponential, logarithmic, sine, cosine, rational, polynomial, and power functions and their transformations, including $af(x)$ , $f(x) + d$ , $f(x - c)$ , $f(bx)$ for specific values of $a$ , $b$ , $c$ , and $d$ , in mathematical and real-world problems;
✓	(H) graph $\arcsin x$ and $\arccos x$ and describe the limitations on the domain;
✓	(I) determine and analyze the key features of exponential, logarithmic, rational, polynomial, power, trigonometric, inverse trigonometric, and piecewise defined functions, including step functions such as domain, range, symmetry, relative maximum, zeros, asymptotes, and intervals over which the function is increasing or decreasing;
	(J) analyze and describe end behavior of functions, including exponential, logarithmic, rational, polynomial, and power functions, using infinity notation to communicate this characteristic in mathematical and real-world problems;
	(K) analyze characteristics of rational functions and the behavior of the function around the asymptotes, including horizontal, vertical, and oblique asymptotes;
	(L) determine various types of discontinuities in the interval $(-\infty, \infty)$ as they relate to functions and explore the limitations of the graphing calculator as it relates to the behavior of the function around discontinuities;
	(M) describe the left-sided behavior and the right-sided behavior of the graph of a function around discontinuities;
	(N) analyze situations modeled by functions, including exponential, logarithmic, rational, polynomial, and power functions, to solve real-world problems;
✓	(O) develop and use a sinusoidal function that models a situation in mathematical and real-world problems; and
✓	(P) determine the values of the trigonometric functions at the special angles and relate them in mathematical and real-world problems.
	<b>(3) Relations and geometric reasoning.</b> The student uses the process standards in mathematics to model and make connections between algebraic and geometric relations. The student is expected to:
✓	(A) graph a set of parametric equations;
✓	(B) convert parametric equations into rectangular relations and convert rectangular relations into parametric equations;

✓	(C) use parametric equations to model and solve mathematical and real-world problems;
✓	(D) graph points in the polar coordinate system and convert between rectangular coordinates and polar coordinates;
✓	(E) graph polar equations by plotting points and using technology;
✓	(F) determine the conic section formed when a plane intersects a double-napped cone;
✓	(G) make connections between the locus definition of conic sections and their equations in rectangular coordinates;
✓	(H) use the characteristics of an ellipse to write the equation of an ellipse with center $(h, k)$ ; and
✓	(I) use the characteristics of a hyperbola to write the equation of a hyperbola with center $(h, k)$ .
	<b>(4) Number and measure.</b> The student uses process standards in mathematics to apply appropriate techniques, tools, and formulas to calculate measures in mathematical and real-world problems. The student is expected to:
✓	(A) determine the relationship between the unit circle and the definition of a periodic function to evaluate trigonometric functions in mathematical and real-world problems;
✓	(B) describe the relationship between degree and radian measure on the unit circle;
✓	(C) represent angles in radians or degrees based on the concept of rotation and find the measure of reference angles and angles in standard position;
✓	(D) represent angles in radians or degrees based on the concept of rotation in mathematical and real-world problems, including linear and angular velocity;
✓	(E) determine the value of trigonometric ratios of angles and solve problems involving trigonometric ratios in mathematical and real-world problems;
✓	(F) use trigonometry in mathematical and real-world problems, including directional bearing;
✓	(G) use the Law of Sines in mathematical and real-world problems;
✓	(H) use the Law of Cosines in mathematical and real-world problems;
✓	(I) use vectors to model situations involving magnitude and direction;
✓	(J) represent the addition of vectors and the multiplication of a vector by a scalar geometrically and symbolically; and
✓	(K) apply vector addition and multiplication of a vector by a scalar in mathematical and real-world problems.
	<b>(5) Algebraic reasoning.</b> The student uses process standards in mathematics to evaluate expressions, describe patterns, formulate models, and solve equations and inequalities using properties, procedures, or algorithms. The student is expected to:
	(A) evaluate finite sums and geometric series, when possible, written in sigma notation;
	(B) represent arithmetic sequences and geometric sequences using recursive formulas;
	(C) calculate the $n$ th term and the $n$ th partial sum of an arithmetic series in mathematical and real-world problems;
	(D) represent arithmetic series and geometric series using sigma notation;
	(E) calculate the $n$ th term of a geometric series, the $n$ th partial sum of a geometric series, and sum of an infinite geometric series when it exists;
	(F) apply the Binomial Theorem for the expansion of $(a + b)^n$ in powers of $a$ and $b$ for a positive integer $n$ , where $a$ and $b$ are any numbers;
	(G) use the properties of logarithms to evaluate or transform logarithmic expressions;
	(H) generate and solve logarithmic equations in mathematical and real-world problems;
	(I) generate and solve exponential equations in mathematical and real-world problems;
	(J) solve polynomial equations with real coefficients by applying a variety of techniques in mathematical and real-world problems;
	(K) solve polynomial inequalities with real coefficients by applying a variety of techniques and write the solution set of the polynomial inequality in interval notation in mathematical and real-world problems;
	(L) solve rational inequalities with real coefficients by applying a variety of techniques and write the solution set of the rational inequality in interval notation in mathematical and real-world problems;

✓	(M) use trigonometric identities such as reciprocal, quotient, Pythagorean, cofunctions, even/odd, and sum and difference identities for cosine and sine to simplify trigonometric expressions; and
✓	(N) generate and solve trigonometric equations in mathematical and real-world problems.
	<i>Source: The provisions of this §111.42 adopted to be effective September 10, 2012, 37 TexReg 7109.</i>