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- European | Republican; -

to stand for all Europeans and Republicans taken together, without intending to count twice over the European Republicans. Boole and Venn (his sole living defender) would insist upon our writing

European 4 Non-European Republican,

Non-Republican European + Republican,

The two new authors both side with the majority in this respect.

2. Mr. McColl and I find it to be absolutely necessary to add some new sign to express existence; for Boole's notation is only capable of representing that some description of thing does not exist, and cannot say that anything does exist. Besides that, the sign of equality, used by Boole in the desire to assimilate the algebra of logic to that of number, really expresses, as De Morgan showed forty years ago, a complex relation. To say that

African = Negro

implies two things, that every African is a Negro, and that every Negro is an African. For these reasons, Mr. McColl and I make use of signs of inclusion and of non-inclusion. Thus, I write

Griffin < breathing fire

to mean that every griffin (if there be such a creature) breathes fire; that is, no griffin not breathing fire exists; and I write

Animal  $\geq$  Aquatic,

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