

LOCALIZATION - LOGIC

objects in the external world. See SPACIALI-ZATION

The earliest theory of space localization in the sense of (1) is what Hamilton calls 'the ANGELL and FITE, Psychol. Rev., viii. 225. common dogma of the schools, that the soul is all in the whole body, and all in every one of its parts' (Reid's Works, Suppl. Diss., schaft, localisirte Industrie; Fr. spécialisation 861, note). Then follows the doctrine of (d'audustrie) locale; Ital. industria locale Descartes, that the soul immediately perceives the images in the corporeal phantasy, different communities. viz. the brain. The modern treatment of the subject may be said to start with Herbart in development. The first is where the distinc-Germany and with Bain in England. WOLKMANN, Lehrb. d. Psychol., ii, 117-26; articles they have produced; yet where conand for Bain's view see BAIN, The Senses and sumers live near the producer and are personally the Intellect, 415 ff. Cf. the textbooks of known to him. The second stage is where the

SPACE (perception of). the subject of an event in his own history to reached when increasing facilities of comits position in the time series relatively to the munication make the world one trading compresent moment and to other events, past and munity. Then the localization of trades profuture. See TIME.

localization is comparatively modern. Its the goods of a certain sort that are consumed. detailed treatment begins with the Herbartian throughout the world' (Walker). psychology in Germany. For something of Locke, John. (1632-1704.) Born at the theory see TEMPORAL SIGN.

lish is, perhaps, WARD, art. Psychology, Encyc. family, directing the education of his son and

tion der Gehörsempfindungen; Fr. localisation and in Holland, 1684-9. In 1690 he pubdes sensations auditives; Ital. localizzazione (or lished his famous 'Essay,' and died at Oates in projezione) spaziale delle sensazioni uditive. Essex, Oct. 28, 1704. He is founder of English The reference of sounds to particular localities EMPIRICISM (q.v., also SENSATIONALISM). in space. See SPACIALIZATION.

tion of sounds appears to be conditioned, Locomotion, (2) Bewegungs-(werkzeug, &c.); Fr. primarily, by the relative intensity of the locomotion, locomoteur; Ital. (1) locomozione, waves that reach the two ears. Localization (2) locomotore. (1) The act or power of of sounds is thus a function of BINAURAL moving from place to place. (2) Pertaining HEARING (q. v.). It is doubtful how far the to the mechanism of locomotion. See Movepure auditory perception could have developed MENT, and MUSCLE. without visual perception; and, indeed, no **Logic** [Gr. $\lambda oyuk\eta$]: Ger. Logik; Fr. explanation has as yet been proposed that is logique; Ital. logica. Logic is a science adequate in detail to the observed phenomena. which has not yet completed the stage of

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LEIGH, Nature, xiv. 32 ; SANFORD, Course in Exper. Psychol., expts. 101-3; MATSUMOTO, Yale Studies, v. 1 ff.; SCRIPTURE, ibid., 76 ff.; (E.B.T.)

Localized Industry : Ger. Weltwirthspecializzata. The division of labour between

' Wednay mark off three stages of industrial tion of trades is introduced, and men no Literature: for the Herbartian view see longer consume all or perhaps any part of the See also EXTENSION, and element of personal acquaintance disappears. (G.F.S.-J.M.B.) Production no longer waits for orders, but Localization (in time). The reference by anticipates demand. The third stage is ceeds so far that one country, or perhaps one The question of the conditions of time group of towns, produces the greater part of all

Wrington, Somersetshire, England, he was Literature: Volkmann, Lehrb. d. Psychol., ii. 11-20. There is little written on the Christ Church, Oxford. Secretary to Sir subject by the classical English psycho- Walter Vane at Berlin, &c., 1665-6; formed logists; see, however, JAMES MILL, Analysis, the acquaintance of Ashley, afterwards Earl of chap. x. The best modern reference in Eng- Shaftesbury, 1666. He entered Lord Ashley's Brit., 64-5. See the textbooks of psycho-grandson. As lord chancellor, Shaftesbury gy. **Localization of Sounds:** Ger. Lokalisa-fices. He stayed in France and Italy, 1675-9,

(J.M.B.) Locomotion (1), and (2) Locomotor [Lat. Our apprehension of the distance and direc- locus, place, + motio, a moving]: . Ger. (1)

Literature: PREYER, Pflüger's Arch., xl.; Von KRIES, Zeitsch. f. Psychol., i. 235, 488; MÜNSTERBERG, Beitr. z. exper. Psychol., ii, a hundred definitions of it have been given. and (with PIERCE) Psychol. Rev., i. 461; RAY- It will, however, generally be conceded that

commencement of such a classification of called logica docens. See REASONING.

which, setting out with such assumptions as appeal was frequently made to authority.

its central problem is the classification of Diogenes Laertius, Aristotle divided logic arguments, so that all those that are bad are into three parts, of which one was $\pi \rho i s \kappa \rho i \sigma w$). thrown into one division, and those which are This word, used by Plato (who divides all good into another, these divisions being knowledge into epitactic and critic), was defined by marks recognizable even if it be adopted into Latin by the Ramists, and into Kant is emphatic in the expression of the wish

not known whether the arguments are good English by Hobbes and Locke. From the or bad. Furthermore, logic has to divide last it was taken into German by Kant, who good arguments by recognizable marks into always writes it Critik, the initial c being those which have different orders of validity, possibly a reminiscence of its English origin. and has to afford means for measuring the At present it is written Kritik in German. An approach to such a classification is made that the word may not be confounded with by every man whenever he reasons, in the proper critique, a critical essay (Ger. Kritik). [The sense of that term. It is true that the contem- | forms Critique and Critic are used interchangeplation of a state of things believed to be real ably in this work. (Cf. CRITICISM.) (J.M.B.)] may cause the contemplator to believe something It is generally admitted that there is a additional, without making any classifica- doctrine which properly antecedes what we tion of such sequences. But in that case he have called critic. It considers, for example, does not criticize the procedure, nor so much in what sense and how there can be any true as distinctly reflect that it is just. He can, proposition and false proposition, and what consequently, not exercise any control over it. are the general conditions to which thought or Now, that which is uncontrollable is not signs of any kind must conform in order to subject to any normative laws at all; that is, assort anything. Kant, who first raised these it is neither good nor bad; it neither sub- questions to prominence, called this doctrine serves an end nor fails to do so. But it is transcendentale Elementarlehre, and made it only the deliberate adoption of a belief in a large part of his Critic of the Pure Reason. consequence of the admitted truth of some But the Grammatica Speculativa of Scotus is other proposition which is, properly speaking, an earlier and interesting attempt. The comreasoning. In that case the belief is adopted mon German word is Erkenntnisstheorie, because the reasoner conceives that the method sometimes translated EPISTEMOLOGY (q. v.). by which it has been determined would either | It is further generally recognized that in no analogous case lead to a false conclusion another doctrine follows after critic, and which from true premises, or, if steadily adhered to, belongs to, or is closely connected with, logic. would at length lead to an indefinite approxi- Precisely what this should contain is not mation to the truth, or, at least, would assure agreed; but it must contain the general conthe reasoner of ultimately attaining as close ditions requisite for the attainment of truth. an approach to the truth as he can, in any Since it may be held to contain more, one way, be assured of attaining. In all reason- hesitates to call it heuristic. It is often called ing, therefore, there is a more or less conscious Method; but as this word is also used in the con-. reference to a general method, implying some crete, methodic or methodeutic would be better. For deciding what is good logic and what arguments as the logician attempts. Such bad, appeal is made by different writers to a classification of arguments, antecedent to one or more, generally several, of these eight any systematic study of the subject, is called sources: to direct dicts of consciousness, to the reasoner's logica utens, in contradistinction psychology, to the usages of language, to to the result of the scientific study, which is metaphysical philosophy, to history, to everyday observation, to mathematics, and to some That part of logic, that is, of logica docens, process of dialectic. In the middle ages that every assertion is either true or false, The appeal to direct consciousness consists and not both, and that some propositions in pronouncing certain reasoning to be good may be recognized to be true, studies the or bad because it is felt to be so. This is constituent parts of arguments and produces a very common method. Sigwart, for example, a classification of arguments such as is above bases all logic upon our invincible mental described, is often considered to embrace the repulsion against contradiction, or, as he calls whole of logic; but a more correct designa- it, 'the immediate feeling of necessity' (Logic, tion is Critic (Gr. «perisé). According to § 3, 2). Those who think it worth while to

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make any defence at all of this proceeding stinct without any logical control at all, which urge, in effect, that, however far the logician would be as much as to say that we ought however, to be noted that among the dicta of validity of reasoning consists, and whether the direct consciousness, many pronounce certain reasoning in question possesses those characters. reasonings to be bad. If, therefore, such dicta are to be relied upon, man not only usually has every appeal to any fact relating to the mind. certain propositions in Euclid were studied mind as doubt, and the fact that the mind for two thousand years by countless keen struggles to escape from doubt. Even facts minds, all of whom had an immediate feeling like these require to be carefully examined by of evidence concerning their proofs, until at the logician before he uses them as the basis last flaws were detected in those proofs, and of his doctrine. But many logicians have are now admitted by all competent persons; gone much further, and have avowedly based and it is claimed that this illustrates how far their systems upon one or another theory of from possible it is to make direct appeal to psychology. Another class of logicians have a definitive pronouncement. Besides, say professed to base logic upon a psychological those who object to this method, all reasoning theory of cognition. Of course, if this is done, and inquiry expects that there is such a thing such psychological doctrine is placed above as the truth concerning whatever question logical criticism, or, at any rate, above logical may be under examination. Now, it is of the support. For if the truth of a conclusion is very essence of this 'truth,' the meaning of known only from certain premises, it cannot the expectation, that the 'truth' in no wise be used to support those premises. Now, it depends upon what any man to whom direct may be doubted whether psychology is not, of appeal can be made may opine about that all the special sciences, the one which stands question. A fortiori it does not depend upon most in need of appeal to a scientific logic. whether I am satisfied with it or not. It is Appeals to the usages of language are further insisted that there can be no genuine extremely common. They are made even by is actually doubted; and no sooner is it | 'in order to free the mind from the trammels ness has revoked her dictum in its favour, if difficult to see what can be hoped for from she ever made any. It is, indeed, main- such a proceeding, unless it be to establish a tained that so far from true is it that every psychological proposition valid for all minds. system of logic must be based upon any in- But to do this, it would be necessary to look stinctive recognition of good and bad rea- beyond the small and very peculiar class of soning, that it is quite impossible for any Aryan languages, to which the linguistic reasoning to be based upon such recognition knowledge of most of those writers is confined. in respect to that same reasoning. In reason- The Semitic languages, with which some of ing, a man may feel sure he is right; but to them are acquainted, are too similar to the 'rest' that confidence on nothing but itself is Aryan greatly to enlarge their horizon. Moreto rest it on nothing at all. If the fact that we over, even if other languages are examined, must use our reasoning instinct in criticizing the value of any logical inferences from them reasoning proves that we must appeal to is much diminished by the custom of our

may push his criticisms of reasoning, still, in not to reason at all. A man cannot criticize doing so, he must reason, and so must ulti- every part of his reasoning, since he cannot mately rely upon his instinctive recognition criticize the act of reasoning he is performing of good and bad reasoning. Whence it follows in the criticism, it is true. But he can criticize that, in Sigwart's words, 'every system of steps whose validity he doubts; and in doing logic must rest upon this principle.' It is, so, ought to consider in what characters the

Under an appeal to psychology is not meant a tendency to reason right, but also some- For it is, for logical purposes, important to times has a tendency to reason wrong; and if discriminate between facts of that description that be so, the validity of a reasoning cannot which are supposed to be ascertained by the consist in a man's having a tendency to reason systematic study of the mind, and facts the in that way. Some say that the validity of knowledge of which altogether antecedes such reasoning consists in the 'definitive dictum' study, and is not in the least affected by it; of consciousness; but it has been replied that such as the fact that there is such a state of

criticism of a reasoning until that reasoning those who use algebraical notation in logic actually doubted than we find that conscious of speech' (Schröder, Logik, i. p. iii). It is nothing else in such criticism, it qually proves grammarians of violently fitting them to the that we ought to follow the lead of that in- Procrustean bed of Aryan grammar.

appeals to psychological results applies with than those which were expressed in the prefar greater force to appeals to metaphysical cept. These being abstractly stated, and philosophy, which, it will generally be con- being generalized, so as to apply to every ceded, can hardly take a step with security diagram constructed according to the same unless it rests upon the science of logic. Nevertheless, a great many logical treatises of various colours make it their boast that they depends upon a kind of inward observation, are built upon philosophical principles.

must be admitted to have great weight. altogether illusory. They will naturally be out of place in a system | The generally received opinion among proof logic which professes to demonstrate from fessors of logic is that all the above methods There is probably room for dispute as to recognized.

whether logic need assert anything at all as an Literature: the history of logic in Western absolute matter of fact. If it does not, any Europe, down to the revival of learning, is appeal to experience would seem to be irre- given by PRANTL, Gesch. d. Logik im levant. If it does, still the opinion may Abendlande. Upon the points upon which be that such assertions of logic are of so this author touches, he always affords valuexceedingly broad and slight a nature that the able information, though his judgments are universal experience of every man's every day peremptory and slashing. Unfortunately, he and hour puts them beyond all doubt-such omits much which was regarded by the experiences as that the world presents appear- authors of whom he treats as most imporances of variety, of law, and of the real action fant, because he does not himself so regard of one thing upon another. As appearances, it. He also omits much which would be inthese things do not seem likely ever to be teresting to a reader taking a broader condoubted. If logic has need of any facts, and ception of logic. It is hardly necessary to if such facts will suffice, no objection can well say that upon some large subjects his views he made to an appeal to them.

and pure mathematics in its modern treat- but there are notices good as far as they go ment is almost evanescent, as may be seen in in UEBERWEG, Syst. d. Logik (Eng. trans.); Dedekind's Was sind und was sollen die Zahlen in the much earlier work of BACHMANN, (1888, Eng. trans. 1901). There are, however, Syst. d. Logik (1828); in HAMILTON, Lects. departments of logic, such as the logic of pro- on Logic ; and for later work in B. ERDMANN, bable inference (if that be regarded a part of Logik. CH. SIGWART, Logic (Eng. trans.), logic), in which appeal is sometimes made to and WUNDT, Logik, may also be profitably mathematical results, such as Bernoulli's law of consulted. See under the logical topics generhigh numbers. Itseems to be the general opinion ally (e.g. EMPIRICAL LOGIC, FORMAL LOGIC, that nothing so difficult as mathematics can JUDGMENT, and PROPOSITION); and also be admitted into, or be appealed to by, the BIBLIOG, C. science of logic, which has the peculiarity of consisting chiefly of truisms.

In mathematical reasoning there is a sort | of observation. For a geometrical diagram logique exacte; Ital. logica esatta. The docor array of algebraical symbols is constructed trine that the theory of validity and strength according to an abstractly stated precept, and of reasoning ought to be made one of the between the parts of such diagram or array ('exact sciences,' that is, that generalizations

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certain initial assumptions that the kinds of may properly be used on occasion, the appeal reasoning it recommends must be accepted. to mathematics, however, being less generally

are controverted. Of the modern develop-The boundary between some parts of logic ment of logic there is no satisfactory history; (C.S.P., G.L.F.)

Logic (Hegel's Logik): see HEGEL'S TER-MINOLOGY, II b.

Logic (exact): Ger. exakte Logik; Fr.

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from ordinary experience ought, at an early algebra which brings along with it hundreds point in its exposition, to be stated in a form of purely formal theorems of no logical import from which by mathematical, or expository, whatever must be admitted, even by the REASONING (q. v.), the rest of the theory can inventor of it, to be extremely defective in be strictly deduced; together with the attempt that respect, however convenient it may be to carry this doctrine into practice.

Pascal (1623-62), Nicolas Bernoulli (1687- over speech in forcing us to reason explicitly 1759), Euler (1708-83), Ploucquet (1716- and definitely, if at all. . In that way it may 90), Lambert (1728-77), La Place (1749- afford very considerable aid to analysis. It has 1827), De Morgan (1806-71), Boole (1815- been employed with great advantage in the 64), and many, others; and a few men in analysis of mathematical reasonings. different countries continue the study of the Algebraic reasoning involves intuition just problems opened by the last two named as much as, though more insidiously than, logicians, as well as these of the proper does geometrical reasoning; and for the infoundations of the doctrine and of its appli- vestigation of logic it is questionable whether cation to inductive reasoning. The results of the method of graphs is not superior. Graphs this method, thus far, have comprised the cannot, it is true, readily be applied to cases development of the theory of probabilities, the of great complexity; but for that very reason logic of relatives, advances in the theory of they are less liable to serve the purposes of inductive reasoning (as it is claimed), the the logical trifler. In the opinion of some syllogism of transposed quantity, the theory exact logicians, they lead more directly to the of the Fermatian inference, considerable steps ultimate analysis of logical problems than towards an analysis of the logic of continuity any algebra yet devised. See LOGICAL DIAand towards a method of reasoning in topical GRAM (OR GRAPH). geometry, contributions towards several It is logical algebra, however, which has branches of mathematics by applications of chiefly been pursued. De Morgan invented

that such a project, which is much more application of ordinary algebra to the treatconsonant with the ideas of the opponents of ment of all deductive reasoning not turning exact logic than with those of its serious upon any relations other than the logical students, can ever be realized. The real aim relations between non-relative terms. By is to find an indisputable theory of reasoning means of this simple calculus, he took some by the aid of mathematics. The first step in great steps towards the elucidation of probable the order of logic towards this end (though reasoning; and had it not been that, in his not necessarily the first in the order of inquiry) pre-Darwinian day, the notion that certain is to formulate with mathematical precision, subjects were profoundly mysterious, so that

mentary a character to be of mathematical logicians of to-day are, from the nature of interest, and too superficial to be of logical the case, followers of Boole. They have

for certain purposes. On the other hand, it This method was pursued, in the past, by is indisputable that algebra has an advantage

exact' logic, the logical graphs called after a system of symbols, which had the signal Euler and other systems for representing in advantage of being entirely new and free from + intuitional form the relations of premises to all associations, misleading or otherwise. conclusions, and other things of the same Although he employed them for synthetical purposes almost exclusively, yet the great There are those, not merely outside the generality of some of the conceptions to ranks of exact logic, but even within it, who which they led him is sufficient to show that seem to suppose that the am is to produce they might have been applied with great . a calculus, or semi-mechanical method, for advantage in analysis. Boole was led, no performing all reasoning, or all deductive doubt from the consideration of the principles. inquiry; but there is no reason to suppose of the calculus of probabilities, to a wonderful definiteness, and simplicity, the general facts of it was hopeless, if not impious, to seek to experience which logic has to take into account. penetrate them, was still prevalent in Great The employment of algebra in the investi- Britain, his instrument and his intellectual gation of logic is open to the danger of force were adequate to carrying him further degenerating into idle trifling of too rudi- than he actually went. Most of the exact interest. It is further open to the danger modified his algebra by disusing his addition, that the rules of the symbols employed may subtraction, and division, and by introducing be mistaken for first principles of logic. An a sign of logical aggregation. This was first

tion. Inasmuch as this might easily be read as three signs, it would-perhaps, be better to join the two dots by a light curve, thus Ψ . so as to fit it for the logic of relatives. The But this is not sufficiently accurate for the See RELATIVES (logic of).

Certain terms of exact logic may be defined as follows :---

or more terms or propositions, called aggre- often does fulfil the function mentioned; but gants, to produce an aggregate term or propo- it is only an accidental one, and its essential sition which is true of everything of which function is quite different. Thus, the propoany aggregant is true, and false of everything sition 'Some favoured patriarch is translated' of which all the aggregants are false. It is is essentially the same as 'A translated opposed to composition, which is the opera- favoured patriarch is'; and 'Every mother is tion of producing from two or more terms or a lover of that of which she is a mother' is propositions, called the components, a new the same as 'A mother of something not term or proposition, called their compound, loved by her is not.' In the second and which is true of all of which all the compo- fourth forms, the copula connects no terms; neuts are true, and false of all of which any but if it is dropped, we have a mere term

by some logicians to 'disjunctive,' because the hearer, between the mind as appealing to Gellius, understood to by that one, and as so appealed to, or there can be no commu-one only, of the alternation is true. At the nication, or 'common ground,' at all. The same time, the standard traditional example universe is, thus, not a mere concept, but is of a disjunctive was 'Socrates currit vel Plato | the most real of experiences. Hence, to put disputat,' and the rule was 'Ad veritatem a concept into relation to it, and into the disjunctivac sufficit alteram partem esseveram.' relation of describing it, is to use a most Nevertheless, the narrower sense was also peculiar sort of sign or thought; for such

elements is associative if, and only if, in tially does. This it may do in three ways: combining the result with a third element, first, by a vague reference to the universe it makes no difference whether the middle collectively; second, by a reference to all the element be first combined with the last and individuals existent in the universe distri-the result with the first, or the other way, so butively; third, by a vague reference to an long as the order of sequence is preserved. individual of the universe selectively. 'It is Addition and multiplication are associative, broad daylight, I exclaim, as I awake. My uniwhile involution is not so; for ten to the verse is the momentary experience as a whole. three-square power is a milliard, while ten It is that which I connect as object of the cube squared is only a million. An associa- composite photograph of daylight produced tive algebra is an algebra in which multipli- in my mind by all my similar experiences.

elements are united is said to be commutative the universe. Every such individual is said if, and only if, it makes no difference which is to be coexistent only with what, so far as it

LOGIC done by Jevons; and he proposed . . , a sign taken first. Thus, because twice three is thrice of division turned up, to signify this opera- two, numerical multiplication is commutative. Composition : see Aggregation, above. Compound : see Aggregation, above. Copula is often defined as that which Some use the sign + for logical aggregation. expresses the relation between the subject-The algebra of Boole has also been amplified term and the predicate-term of a proposition.

system is, however, far from being perfect. purposes of exact logic. Passing over the objection that it applies only to categorical propositions, as if conditional and copulative propositions had no copula, contrary to logical Aggregation. The operation of uniting two tradition, it may be admitted that a copula instead of a proposition. Thus the essential Absorption, law of (Ger. Absorptionsgesetz). office of the copula is to express a relation of The proposition that if of two aggregants one a general term or terms to the universe. contains the other as a component, the aggre- The universe must be well known and mutually known to be known and agreed to Alternative proposition. A term preferred exist, in some sense, between speaker and icero and Aulus its own further consideration and the mind recognized, and the term alternative is per- a relation must, if it subsist, exist quite otherwise than a relation between mere con-Associative. An operation combining two cepts. This, then, is what the copula essen-Secondly, 'Every woman loves something' is Commutative. An operation by which two a description of every existing individual in

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is a woman at all, is sure to be a lover of ever. So understood, it is the abstract copula some existing individual. Thirdly, 'Some of De Morgan (Camb. Philos. Trans., x. 339). this; but it is manifestly indisputable. Those relative r may be, the copula is called the copula logicians belong to two classes: those who of inclusion, used by C. S. Peirce, Schröder, think that logic ought to take account of the and others. De Morgan uses a copula dedifference between one kind of universe and fined as standing for any relation both transianother (in which case, several other substan- tive and convertible. The latter character tiae of propositions must be admitted); and consists in this, that whatever terms I and those who hold that logic should distinguish J may be, if we represent this copula by is between propositions which are necessarily in black=letter, then from 'I is J' it follows true or false together, but which regard the that 'J is I.' From these two propositions, fact from different aspects. The exact we conclude, by Barbara, that 'I is I.' Such logician holds it to be, in itself, a defect in copulas are, for example, 'equal to,' and 'of a logical system of expression, to afford the same colour as.' For any such copula different ways of expressing the same state there will be some relative term r, such that of facts; although this defect may be less the proposition 'S is P' will be precisely important than a definite advantage gained equivalent to 'S is r to everything, and only by it. The copulative proposition is in a to everything, to which P is r.' Such a similar way equivalent to a particular cate- copula may be called a copula of correlative gorical. Thus, to say 'The man might not identity. If the last proposition follows from be able voluntarily to act otherwise than the last but one, no matter what relative r may physical causes make him act, whether he be, the copula is the copula of identity used try or not,' is the same as to say that there by Thomson, Hamilton, Baynes, Jevons, and is a state of things hypothetically admissible many others. in which a man tries to act one way and It has been demonstrated by Peirce that voluntarily acts another way in consequence the copula of inclusion is logically simpler of physical causes. As to hypotheticals ut than that of identity. nunc, they refer to no range of possibility, but Diagram : see LOGICAL DIAGRAM. simply to what is true, vaguely taken collectively.

of the copula in relating the subject-term to additional term; opposed to a syllogism, in the predicate-term is a secondary one, it is which from a copulative proposition a proponevertheless necessary to distinguish between sition is inferred from which a term is elimicopulas which establish different relations nated. between these terms. Whatever the relation is, it must remain the same in all propositional forms, because its nature is not expressed in the proposition, but is a matter of established convention. With that proviso, the copula may imply any relation whatso-

favoured patriarch is translated' means that A transitive copula is one for which the mood a certain description applies to a select indi- Barbara is valid. Schröder has demonstrated vidual. A hypothetical proposition, whether the remarkable theorem that if we use is in it be conditional (of which the alternative, or small capitals to represent any one such disjunctive, proposition is a mere species, or copula, of which 'greater than' is an vice versa, as we choose to take it) or copula- example, then there is some relative term r, tive, is either general or ut nunc. A general such that the proposition 'S is P' is precisely conditional is precisely equivalent to a uni- equivalent to 'S is r to P and is r to whatversal categorical. 'If you really want to be ever P is r to.' A copula of correlative inclugood, you can be,' means ' Whatever determi- sion is one for which both Barbara and the nate state of things may be admissibly formula of identity hold good. Representing supposed in which you want to be good is any one such copula by is in italics, there is a a state of things in which you can be good.' relative term r, such that the proposition The universe is that of determinate states of 'S is P' is precisely equivalent to 'S is r to things that are admissible hypothetically. It whatever P is r to.'. If the last proposition is true that some logicians appear to dispute follows from the last but one, no matter what

Dialogism. A form of reasoning in which from a single premise a disjunctive, or alterna-Although it is thus plain that the action tive, proposition is concluded introducing an

Syllogism.

All men are animals, and all animals are mortal;

.: All men are mortal. Dialogism.

Some men are not mortal;

. Either some men are not animals, or in Logic; Pop. Sci. Mo., xii. I; and Proc.

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Dimension. An element or respect of SCIENTIFIC METHOD. extension of a logical universe of such a nature that the same term which is individual in one such element of extension is not so in another. Thus, we may consider different persons as individual in one respect, while they may be divisible in respect to time, and in respect to different admissible hypothetical states of things, &c. This is to be widely spective of any facts except those of which distinguished from different universes, as, for logic needs to take cognizance, such as the example, of things and of characters, where facts of doubt, truth, falsity, &c. any given individual belonging to one cannot | belong to another. The conception of a freedom from all contradiction, explicit ormultidimensional logical universe is one of implicit; and any attempt to reform the the fecund conceptions which exact logic owes inaccuracy would only bring confusion. to O. H. Mitchell. Schröder, in his then second volume, where he is far below himself in many respects, pronounces this conception 'untenable.' But a doctrine which has, as a examination of every individual of the class matter of fact, been held by Mitchell, Peirce, to which the examination relates. Thus, and others, on apparently cogent grounds, conclusions from a census are logical inducwithout meeting any attempt at refutation in tions. While this mode of inference is a about twenty years, may be regarded as being, degenerate form of induction, it also comes ·be held.

Dyadic relation. A fact relating to two senses, rendering it almost useless. individuals. Thus, the fact that A is similar to B, and the fact that A is a lover of B, and Most usually so defined, but seldom so emthe fact that A and B are both men, are ployed. So far as this definition is distinct, dyadic relations; while the fact that A gives it makes logical truth a synonym for logical B to C is a triadic relation. Every relation possibility; but, no doubt, more is intended of one order of relativity may be regarded as a relative of another order of relativity if desired. Thus, man may be regarded as man of logic; in particular, in a concept, concoexistent with, and so as a relative expressing sistency; in an inference, validity; in a a dyadic relation, although for most purposes proposition, agreement with assumptions.

Index (in exact logic): see sub verbo. Many other technical terms are to be found d. reinen Vernunft, 1st ed., 294). in the liferature of exact logic.

Literature: for the study of exact logic in proposition with the reality, so far as the its more recent development, excluding proba- proposition asserts anything about the reality. bility, the one quite indispensable book is Opposed, on the one hand, to metaphysical SCHRÖDER, Algebra d. Logik; and the truth, which is an affection of the ens, and on the bibliography therein contained is so exhaus- other hand to ethical truth, which is telling tive that it is unnecessary to mention here what a witness believes to be true (Burgersany publications previous to 1890. Schröder's dicius, Inst. Met., chap. xviii). pains to give credit in full measure, pressed Logical parts and whole. Parts and whole down and running over, to every other of logical extension. student is hardly less remarkable than Logical reasoning. Reasoning in accordthe system, completeness, and mathematical ance with a LEADING PRINCIPLE (q. v.) which power of his work, which has been reviewed thorough analysis, discussion, and experience by C. S. PEIRCE in the Monist, vii. 19-40, have shown must lead to the truth, in so far

Amer. Acad. Arts and Sci., vii. 287. Cf. (C.S.P.) Logic (of chance): see PROBABILITY. Logic (of emotion): see TERMINOLOGY, English, 'Affective Logic.' Logic (social) :... soo SOCIAL LOGIC. Logic (symbolic): see SYMBOLIC LOGIC. Logical [Lat. logicalis, from logica, logic]: Ger. logisch ; Fr. logique; Ital. logico. Irre-

Logical possibility is, according to usage,

Logical necessity is the necessity of that whose contrary is not logically possible. Logical induction is an induction based on for the present, at any rate, tenable enough to into the class of dilemmatic reasoning.

Logical truth is a phrase used in three 1. The harmony of a thought with itself. (Hamilton, Lects. on Logic, xxvii). 2. The conformity of a thought to the laws

it will be regarded as a monad or non-relative This would better be called mathematical truth, since mathematics is the only science which aims at nothing more (Kant, Krit.

3. More properly, the conformity of a

171-217. See also C. S. PEIRCE, Studies as it is relied upon. But what Aristotle

LOGICAL DIAGRAM - LOGICAL MACHINE

understood by a logical demonstration may be if every X is r to a Y, and every Y is r to seen in his De generatione animalium, Lib. II. a Z, every X is r to a Z. Now, it is easily

synthetic reasoning, that is, induction and rules, implies neither more nor less than to analogy; for hypothetic reasoning was not say that there is a relation l, such that, recognized as reasoning at all. The uni- whatever individuals A and B may be, formity of nature is called the principle of | If nothing is in the relation l to A with-

parts.

Logical distinctness. That distinctness which results from logical analysis.

Logical actuality. Kant, in the Logik by Jäsche (Einleitung, vii), defines logical a system of graphs, we must find some spatial actuality as conformity to the principle of relation by which it shall appear plain to the sufficient reason, consisting of the cognition eye whether or not there is anything that is having reasons and having no false conse- in that relation to one thing without being in quences; and he makes this, along with that relation to the other. The popular logical possibility, to constitute logical truth, Euler's diagrams fulfil one-half of this condiwhich is thus used in its second sense. But tion well by representing A as an oval inside in the Critic of the Pure Reason, in discussing the oval B. Then, l is the relation of being the functions of judgments (1st ed., 75), he included within; and it is plain that nothing says that an assertoric proposition asserts can be inside of A without being inside B. logical actuality (Wirklichkeit, which Max The relation of the copula is thus represented Müller wrongly translates 'reality'), and by the spatial relation of 'enclosing only what makes this phrase synonymous with logical is enclosed by.' In order to represent the proper, sense).

genus and specific difference. Ockham and his some existing individual. In this case the followers objected to the designation on the subject and predicate ovals must be drawn to ground that the logician, as such, had no occa- intersect each other, in order to avoid assertsion to define any ordinary term, such as man ing too much. If an oval already exists (Tractatus logices, Pt. I. chap. xxvi). (C.S.P.) cutting the space in which the dot is to be logische Figur; Fr. diagramme logique; of that oval, to show that it is doubtful on Ital. diagramma logico. A diagram composed which side it belongs; or, if an oval is to be of dots, lines, &c., in which logical relations drawn through the space where a dot is, it are signified by such spatial relations that should be drawn through the dot; and it should the necessary consequences of these logical further be remembered that if two dots lie on relations are at the same time signified, or the boundaries of one compartment, there is can, at least, be made evident by transforming nothing to prevent their being identical. the diagram in certain ways which conven- The relation of negation here appears as

shall represent ordinary syllogisms, it is only | xi. necessary to find spatial relations analogous to the relations expressed by the copula of Fr. machine logique; Ital. machine logistiche inclusion and its negative and to the relation (E.M.). An instrument devised to facilitate of negation. Now all the formal properties by mechanical means the handling of logical of the copula of inclusion are involved in the symbols or diagrams. principle of identity and the dictum de omni. That is, if τ is the relation of the subject of merit attention:a universal affirmative to its predicate, then, whatever terms X, Y, Z may be,

Every X is.r to an X; and

proved by the logic of relatives, that to say Logical presumption. A Wolffian term for that a relation r is subject to these two

out being also in the same relation l to B, Logical division. Division into logical then A is in the relation r to B; and conversely, that,

If A is r to B, there is nothing that is l to A except what is l to B.

Consequently, in order to construct such truth (which is thus used in its third, and negation of the copula of inclusion (which, unlike that copula, asserts the existence of its Logical definition. A strict definition by subject), a dot may be drawn to represent Logical Diagram (or Graph): Ger. placed, the latter should be put on the line 'entirely outside of.' For a later practical In order to form a system of graphs which improvement see Venn, Symbolic Logic, chap. (C.S.P.)

Logical Machine: Ger. logische Machina;

There are three such instruments which

(1) The first was constructed by W. Stanley Jevons in 1869 (announced in his Substitution of Similars, 1869. 60; described in Philos. 28

