# Statistical Error Components Frameworks for Modeling Autonomous Systems Safety

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### Introduction

Autonomous systems safety includes several considerations with respect to methodology, modeling, and interpretation of findings:

- · Diversity and complexity in autonomous systems architecture
  - Diversity gives rise to unobserved heterogeneity
  - Complexities arise from nonlinearities in system interactions
- Autonomous systems safety is a complex, probabilistic challenge
- System parameters would be statistically biased, can compromise predictive accuracy, and would limit model portability

# **Modeling Results**

Significant variables in autonomous involved crashes included:

- Traffic control type (signalized versus stop controlled)
- Driver contributing factors (inattention/disregarding)
- Road function (city street/interstate/farm-to-market)
- · Fixed object collision involvement
- Nonlinear random parameter effects
  - Proportion of autonomous capable vehicles
  - Number of occupants involved
  - · Number of vehicles involved

Follow the link in the QR code for our published application of this modeling methodology in the context of fixed object collisions.



# Statistical Methodology

The outcome probabilities of a mixed logit model of crash injury severity, which accounts for unobserved heterogeneity in the data and error components, can be derived as:

$$P_n(k) = \frac{EXP[\beta'_{kn}X_{kn} + \sum_{m=1}^{M} d_{km}\theta_m \exp(\gamma'_m he_n)E_{nm}]}{\sum_{q=1}^{K} EXP[\beta'_q X_{qn} + \sum_{m=1}^{M} d_{qm}\theta_m \exp(\gamma'_m he_n)E_{nm}]}$$

where  $P_n(k)$  is the probability of occupant *n* having the crash injury severity *k*,  $\beta_{kn}$  is a vector of estimable parameters,  $X_{kn}$  is a vector of explanatory variables that affect occupant's injury severity level *k*,  $E_{nm}$  is the individual specific underlying random error component,  $d_{km}$  is one if  $E_{nm}$  appears in the severity class *k* and zero otherwise,  $\theta_m$  is the scale factor for the error component, and  $\exp(\gamma'_m he_n)$  is the heterogeneity in variance of the error components, which can be broken down as  $\gamma'_m$ (parameters in the heterogeneity in variance of the error components) and  $he_n$ (individual choice invariant characteristics that produce heterogeneity in the variances of the error components).<sup>1</sup>

#### <sup>1</sup> Greene, W., 2007. NLOGIT version 4.0: reference guide. Econometric Software, Inc.

#### Interpretation and Systems Analysis Challenges

The nonlinear mixed logit uncovers the *nonlinear effects of vehicle technology exposure (example: proportion of autonomous vehicles in a crash, number of occupants, and number of vehicles)*. The nonlinear mixed logit approach is applicable in domains where there are unobserved correlations across multiple severity outcomes.

Challenges associated with autonomous systems safety analysis:

- Big data (data sparsity and statistical adaptations)
- Optimization (improving efficiency and performance)
- · Variable selection (nuanced in the context of automation)

The future of autonomous systems safety necessitates a methodological bridge between AI and statistics at the nexus of:

- · Sociotechnical environment
- Micro and macro policy spectrum
- Geopolitical constraints

